

## Experimental upper bound on superradiance emission from Mn<sub>12</sub> acetate

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We used a Josephson junction as a radiation detector to look for evidence of the emission of electromagnetic radiation during magnetization avalanches in a crystal assembly of Mn<sub>12</sub> acetate. The crystal assembly exhibits avalanches at several magnetic fields in the temperature range from 1.8 to 2.6 K with durations of the order of 1 ms. Although a recent study shows evidence of electromagnetic radiation bursts during these avalanches [J. Tejada *et al.*, Appl. Phys. Lett. **84**, 2373 (2004)], we were unable to detect any significant radiation at well-defined frequencies. A control experiment with external radiation pulses allows us to determine that the energy released as radiation during an avalanche is less than one part in 10<sup>4</sup> of the total energy released. In addition, our avalanche data indicates that the magnetization reversal process does not occur uniformly throughout the sample.

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Single-molecule magnets have been the subject to intense experimental and theoretical investigations during the past decade. At low temperatures, they are bistable and exhibit hysteresis similar to classical magnets.<sup>1–3</sup> In addition, they exhibit fascinating quantum-mechanical properties, such as tunneling between “up” and “down” orientations,<sup>4–7</sup> and interference between tunneling paths.<sup>8</sup> Furthermore, their potential use in quantum computation has been proposed,<sup>9</sup> and experiments with millimeter-wave radiation have been carried out showing that the relaxation rate for magnetization reversal<sup>10,11</sup> and the energy-level populations can be controlled.<sup>12–14</sup> Chudnovsky and Garanin<sup>15</sup> have proposed theoretically that single-molecule magnets could be used to generate superradiance. In a recent experiment, Tejada *et al.* reported that during magnetization avalanches of the molecular magnet Mn<sub>12</sub> acetate millimeter-wave radiation was released.<sup>16</sup> They interpreted the results as evidence of superradiance in the system, in which coherent radiation is produced at frequencies corresponding to transitions between spin states of the molecule. The bolometer used in that study, however, was not sensitive to radiation frequency and so no information about the spectrum of the radiation was available. Here, we report on a study of the fast dynamics of magnetization reversal during avalanches in a crystal assembly of Mn<sub>12</sub> acetate. We used a Josephson junction as a radiation detector, exploiting the ac Josephson effect to create a frequency sensitive detector. We were unable to detect any radiation at the predicted superradiance frequencies during magnetization avalanches. Using external radiation, we were able to set limits on the power and duration of radiation that might be emitted during an avalanche.

Magnetization avalanches in Mn<sub>12</sub> were found at low temperatures<sup>17</sup> even before resonant magnetization tunneling was discovered in this material.<sup>4</sup> In brief, the avalanches are thermal runaway events in which the heat released by the reversal of a metastable spin in an external field induces other spins to flip, rapidly producing a total saturation

of the magnetization. Since tunneling increases the rate at which spins flip, avalanches tend to occur at the magnetic fields where resonant tunneling occurs. Avalanches are seen in samples that are thermally well isolated from their environment: the reduced heat flow out of the sample allows it to reach a temperature high enough to induce an avalanche. Thus avalanches have been seen at very low temperatures,<sup>17</sup> where heat capacities and thermal conductivities are low, and in large crystal assemblies, in which the sample’s surface-to-volume ratio (and hence the thermal conductivity) is small.

The proposed mechanism of superradiance in Mn<sub>12</sub> is represented in Fig. 3 of Ref. 16. The avalanche heats up the sample, creating a transient increase in the population of high-lying levels. This population can decay either by the emission of phonons or of photons. Normally, the former is favored. However, under the proposed superradiance mechanism, if the wavelength of the radiation is large compared to the size of the sample, then the excited spins can decay coherently, leading to a substantial enhancement in the radiation emitted, with the radiation power being proportional to  $N_m^2$ , where  $N_m$  is the number of spins in the radiating state  $|m\rangle$ . The transitions that favor superradiance are between higher-lying levels, where the associated wavelength is large. Tejada *et al.* measured a radiation burst simultaneous with an avalanche. In accordance with the proposed model, if the radiation is due to superradiance, it should primarily comprise a few frequencies corresponding to transitions between high-lying levels. In addition, since superradiance requires coherent transitions between spin states, a substantial fraction of the spins need to reverse simultaneously.

Josephson junctions can be used as sensitive detectors of electromagnetic radiation and can provide spectral information. When monochromatic electromagnetic radiation is incident on a Josephson junction, the current-voltage curve exhibits steps, known as Shapiro steps.<sup>18</sup> The steps occur at

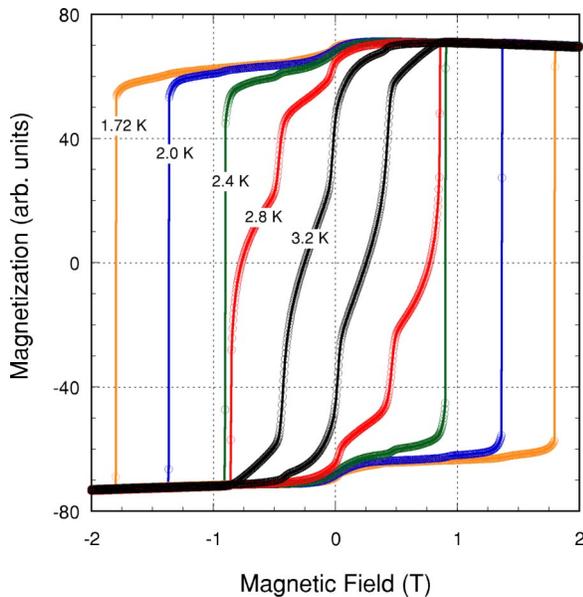


FIG. 1. (Color online) Selected hysteresis loops for a  $\text{Mn}_{12}$  crystal assembly exhibiting avalanches at various temperatures, as indicated.

voltages that are integer multiples of  $h\nu/2e$ , where  $\nu$  is the frequency of the radiation. The Josephson junction is a nonlinear device so that if it is exposed to more than one frequency, it will also show steps at voltages corresponding to the sums and differences of the applied frequencies. If broadband radiation is applied, the steps will be washed out; however, the junction's critical current will still be suppressed.

Several single crystals of  $\text{Mn}_{12}$ , with a total weight of  $\sim 20$  mg ( $\sim 6 \times 10^{18}$  molecules), were assembled together into an approximate cube of side  $\sim 3$  mm. The crystals' anisotropy axes were aligned along the direction of the applied magnetic field to within a few degrees. The magnetization of the crystal assembly was measured by a  $50 \times 50 \mu\text{m}^2$  Hall-bar detector. A Nb/ $\text{AlO}_x$ /Nb Josephson junction was placed several inches away from the sample where the magnetic-field strength is roughly one-tenth of the field that the sample is experiencing. In order to measure the efficiency of the junction as a radiation detector, externally controlled radiation was applied via a rectangular waveguide, ending in a widening waveguide transition that effectively acts as a radiation horn. The distance from the end of the waveguide to the junction was nearly equal to the distance from the sample to the junction.<sup>19</sup>

Hysteresis curves of the crystal assembly were measured at several temperatures, as shown in Fig. 1. Conventional lock-in techniques were used for magnetization measurements while the field was swept at a rate of 5.5 mT/s. The crystal assembly exhibits avalanches at several magnetic fields, which coincide with the fields at which resonant tunneling of magnetization occur, in the temperature range from 1.8 to 2.6 K. The temperature, which is measured with a thermistor mounted near the crystal assembly, rises rapidly up to  $\sim 3.7$  K during these avalanches, in agreement with previous results.<sup>16</sup> Except for the avalanches, the sample be-

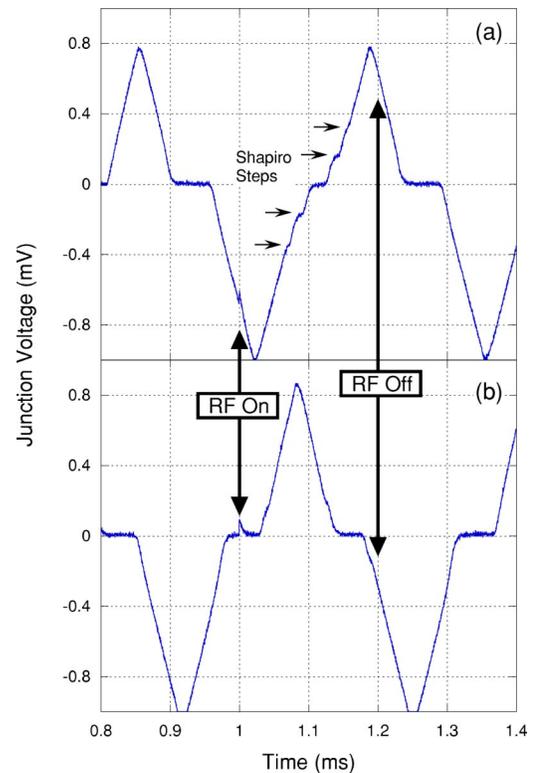


FIG. 2. Voltage drop as a function of time across a Josephson junction while a single 0.2-ms millimeter-wave pulse of 82.52 GHz radiation is applied. The junction is current biased with a triangular waveform. The temperature and the magnetic field at the  $\text{Mn}_{12}$  crystal assembly location are kept at 1.9 K and 1.73 T, respectively. The radiation power is 1.259 mW in (a) and 0.346 mW in (b). The relative horizontal displacement between the data sets in (a) and (b) is an artifact produced by the triggering of the oscilloscope.

haves very much like a single crystal of  $\text{Mn}_{12}$  in terms of the positions and widths of the observed steps.

We use a triangular waveform to current bias the Josephson junction. The frequency of the current drive is set between 2 and 5 kHz with an amplitude of  $\sim 1$  mA. We characterized our junction under identical conditions as those in which we observe avalanches. For example, at a temperature of 1.9 K, the junction's V-I curve was measured with an applied field of 1.73 T (at the sample location). A single 0.2-ms pulse of electromagnetic radiation at a frequency of 82.52 GHz was applied while the junction voltage was measured with a fast digitizing oscilloscope. This frequency is close to one of the predicted superradiance frequencies. The data are shown in Fig. 2. Because of the triangular current bias, each leg of the quasitriangular waveform in the figure represents a V-I curve. In Fig. 2(a), where the external radiation power was 1.259 mW (measured at the end of the waveguide), during the radiation pulse the induced Shapiro steps (marked with arrows) are clearly visible in the voltage-drop across the Josephson junction. An abrupt spike in the junction voltage marks the turn-on time of the pulse. In addition, the critical current is markedly suppressed during irradiation. In Fig. 2(b), the radiation power was reduced to 0.346 mW. Here, some of the Shapiro steps are just barely visible, but the critical current is still noticeably

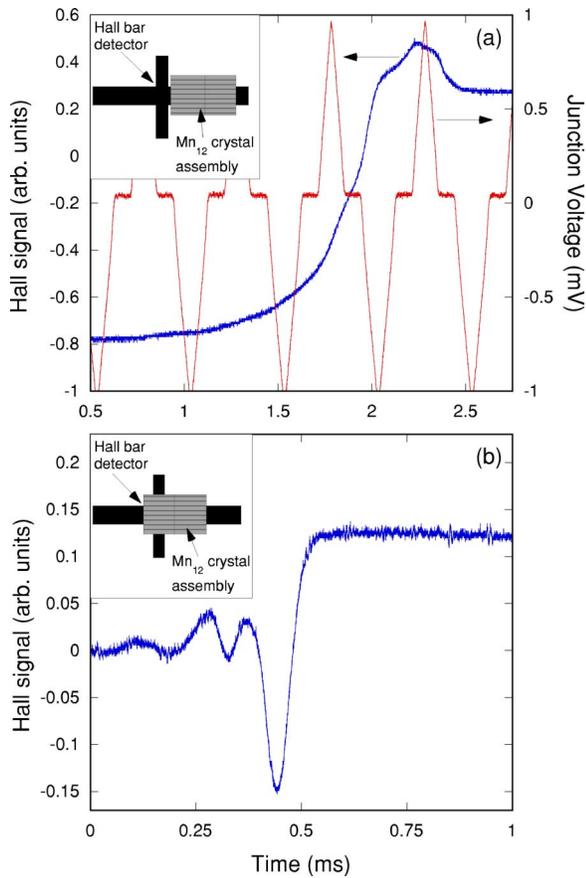


FIG. 3. (Color online) (a) Simultaneously measured magnetization reversal and Josephson junction voltage as a function of time during an avalanche at 2.1 K and at the  $n=3$  tunneling resonance. (b) Magnetization reversal as a function of time during an avalanche at 1.9 K. The relative positions of the crystal assembly and Hall sensor are depicted schematically in the insets.

suppressed. Our junctions can detect pulses as short as 20  $\mu\text{s}$ , but a pulse of at least 50  $\mu\text{s}$  is needed to extract frequency information.

We have found that the magnetization reversal during avalanches occur on millisecond time scales. Therefore, we used a differential amplifier with a settling time of a few  $\mu\text{s}$  to measure the magnetization avalanches. The Hall bar was driven with a dc current and the oscilloscope was triggered by the magnetization avalanche signal, allowing us to simultaneously capture the magnetization of the crystal assembly and the Josephson junction voltage during an avalanche, as shown in Fig. 3(a). The duration of these avalanches increases with temperature. For instance, at 2.5 K the magnetization switches in 3.7 ms, whereas it takes only 1 ms at 1.9 K. These switching times are significantly faster than the 0.1 s reported in Ref. 16. (More recent experiments by the same group give avalanche times consistent with our results.<sup>20</sup>)

Despite numerous measurements on avalanches at different temperatures (and therefore different fields, Fig. 1), we did not observe any indications of a radiation burst in the Josephson junction voltage. In fact, we cannot detect any suppression of the junction's critical current during the

avalanche, as would be expected with broadband radiation. Following Ref. 16, we can estimate the amount of radiation power expected from just one superradiance transition, the  $m=1$  to 2 transition, to be  $P=N_1 h\nu\Gamma_{SR}$ , where  $N_1=N\exp(-U_{\text{eff}}/T)$  is the number of spins in state  $m=1$  (given a total of  $N$  spins) and  $\Gamma_{SR}=N_1\Gamma_1$  is the superradiance decay rate, with  $\Gamma_1$  being the radiative spontaneous decay rate of the  $m=1$  state. Using an effective activation barrier  $U_{\text{eff}}$  of 46 K,  $N\sim 6\times 10^{18}$ ,  $T=3.7$  K, and  $\Gamma_1\sim 1\times 10^{-7}$  s<sup>-1</sup>, we obtain  $P\sim 3$  mW, which should be easily detected by our junction. Assuming the sample reverses coherently, this represents a lower bound on the expected superradiance power since we have taken the temperature to be the maximum measured by our thermometer, located outside the sample. The temperature inside the sample probably reaches a much higher value during the avalanche. The predicted radiation power depends exponentially on temperature and so may be much larger than 3 mW. For example, if we take, e.g.,  $T=4.5$  K, which would yield a magnetic relaxation time on the order of the measured 1 ms, the above calculation would yield a power of  $\sim 200$  mW.

From our experiment we can estimate an upper limit for the fraction of energy that would be emitted as radiation due to superradiance. The total energy released ( $H\cdot\Delta M$ ) for the crystal assembly during the avalanche at 1.9 K and 1.73 T is  $\sim 3.7$  mJ. This translates into an average power of  $\sim 3.7$  W during an avalanche with a typical duration of  $\sim 1$  ms. (Superradiance is expected to last about as long as the avalanche rather than  $1/\Gamma_{SR}$ , because heating from the avalanche repopulates the radiating level.) Considering that our Josephson junctions are sensitive to radiation power levels of at least 0.346 mW, we conclude that less than one part in  $10^4$  of the total energy released is emitted as photons due to superradiance. Put another way, we cannot detect the minimum superradiance power predicted from just one transition even though we have an order of magnitude more sensitivity than necessary to do so. The power levels detected during an avalanche by the InSb bolometer used in Ref. 16 were less than 1  $\mu\text{W}$ ,<sup>20</sup> also much less than expected.

In the foregoing discussion, we assumed that the entire sample reverses its magnetization simultaneously. However, our data indicate that the magnetization reversal process during an avalanche does not occur uniformly throughout the sample. When the magnetization is measured from the edge of the crystal assembly, the measured magnetization changes in a mostly monotonic fashion, although there is noticeable structure [Fig. 3(a)]. However, when the sample is positioned on top of the Hall bar, the signal shows an oscillatory structure that is completely reproducible [Fig. 3(b)]. This indicates that different regions of the sample (perhaps individual crystals) reverse their magnetization sequentially. In fact, similar results have been obtained in the reversal of single Mn<sub>12</sub> crystals in the absence of avalanches.<sup>21</sup> The nonmonotonic behavior in Fig. 3(b) is due to the fact that regions on one side of the detector produce a Hall voltage of opposite sign to that produced by regions on the other side so that when a region of the sample reverses, it can either increase or decrease the Hall signal, depending on its position. Thus, it appears that if superradiance is occurring in Mn<sub>12</sub>, it does not involve the coherent reversal of the whole

assembly. Since the superradiance power is proportional to  $N^2$ , the fact that magnetization reversal occurs sequentially throughout the sample, reducing the effective value of  $N$ , may drastically reduce the amount of radiation power emitted. This would explain why we do not see the predicted  $\sim 3$  mW of power and why the power found in Ref. 20 was so small.

Another reason why the emitted power would be suppressed is that superradiance requires that all of the spins involved have the same transition frequencies to within a natural linewidth. However, because of dipole interactions between molecules, each spin has a different local magnetic field, which in turn leads to a distribution of transition frequencies. In addition, anisotropy parameters for  $\text{Mn}_{12}$  are known to vary from molecule to molecule,<sup>22–27</sup> which would also lead to a distribution in transition frequencies. These mechanisms may sharply reduce the number of spins located within a wavelength of one another that also have the same transition frequency. So, even within a region of the sample that undergoes uniform reversal the effective number of spins participating in superradiance may be much smaller than the number occupying a radiating level.

Our results do not rule out the possibility that superradiance takes place in  $\text{Mn}_{12}$  avalanches. However, if it is occurring, less than  $10^{-4}$  of the total energy released goes into radiation at the predicted superradiance frequencies or the radiation pulse is faster than  $\sim 50$   $\mu\text{s}$ . We have found that these avalanches take place in  $\sim 1$  ms, much faster than previously reported,<sup>16</sup> and the avalanches show a structure indicative of nonuniform magnetization reversal in the crystal assembly. Experiments using frequency sensitive detectors with greater sensitivity should be done to understand the origin of the radiation emitted during avalanches in this system.

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