Abstract:

We associate to a full flag F in an n-dimensional variety X over a field k, a "symbol map" $\mu_F : K(F_X) \to \Sigma^n K(k)$. Here, $F_X$ is the field of rational functions on X, and $K(.)$ is the K-theory spectrum.

We prove a "reciprocity law" for these symbols: Given a partial flag, the sum of all symbols of full flags refining it is 0. Examining this result on the level of K-groups, we derive the following known reciprocity laws: the degree of a principal divisor is zero, the Weil reciprocity law, the residue theorem, the Contou-Carrère reciprocity law (when X is a smooth complete curve) as well as the Parshin reciprocity law and the higher residue reciprocity law (when \(X\) is higher-dimensional).

This is a joint work with Evgeny Musicantov.