Robert Krauthgamer  
Weizmann Institute of Science

Streaming Symmetric Norms via Measure Concentration

Abstract:

A long line of research studies the space complexity of estimating a norm $l(x)$ in the data-stream model, i.e., when $x$ is the frequency vector of an input stream consisting of insertions and deletions of items of $n$ types. I will focus on norms $l$ in $\mathbb{R}^n$ that are *symmetric*, meaning that $l$ is invariant under sign-flips and coordinate-permutations, and show that the streaming space complexity is essentially determined by the measure-concentration characteristics of $l$. These characteristics are known to govern other phenomena in high-dimensional spaces, such as the critical dimension in Dvoretzky's Theorem.

The family of symmetric norms contains several well-studied norms, such as all $l_p$ norms, and indeed we provide a new explanation for the disparity in space complexity between $p \leq 2$ and $p > 2$. We also obtain bounds for other norms that are useful in applications.