The vortex-wave system is a mathematical model for two-dimensional incompressible flows with small regions of concentrated vorticity imbedded upon a continuously distributed background vorticity. The system consists of a coupling of the 2D vorticity equation with the point-vortex system. In this talk we survey known results and recent progress on mathematical analysis of this system.