

Jupiter's atmospheric jet streams extend thousands of kilometres deep

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The depth to which Jupiter's observed east–west jet streams extend has been a long-standing question^{1,2}. Resolving this puzzle has been a primary goal for the Juno spacecraft^{3,4}, which has been in orbit around the gas giant since July 2016. Juno's gravitational measurements have revealed that Jupiter's gravitational field is north–south asymmetric⁵, which is a signature of the planet's atmospheric and interior flows⁶. Here we report that the measured odd gravitational harmonics J_3 , J_5 , J_7 and J_9 indicate that the observed jet streams, as they appear at the cloud level, extend down to depths of thousands of kilometres beneath the cloud level, probably to the region of magnetic dissipation at a depth of about 3,000 kilometres^{7,8}. By inverting the measured gravity values into a wind field⁹, we calculate the most likely vertical profile of the deep atmospheric and interior flow, and the latitudinal dependence of its depth. Furthermore, the even gravity harmonics J_8 and J_{10} resulting from this flow profile also match the measurements, when taking into account the contribution of the interior structure¹⁰. These results indicate that the mass of the dynamical atmosphere is about one per cent of Jupiter's total mass.

The Juno gravity measurements so far have improved the accuracy of the known gravity harmonics J_2 , J_4 , J_6 and J_8 by more than two orders of magnitude^{5,11}. These low-degree even gravity harmonics are mostly affected by Jupiter's interior density structure and its shape¹², and therefore, although the signal from these harmonics may contain a contribution¹³ from the atmospheric and interior flows (ΔJ_n), it is difficult to use these harmonics to infer information about the flows directly. The gravity measurements also revealed north–south asymmetries in Jupiter's gravity field⁵, which are manifested as large values of the odd gravity harmonics J_3 , J_5 , J_7 and J_9 (see Table 1). Because a gas planet rotating as a solid body has no asymmetry between north and south, any non-zero value of the odd J_n must come from dynamics⁶. As the observed cloud-level flow is not hemispherically symmetric (Fig. 1), if enough mass is involved in the asymmetric component of the flow it will produce large odd J_n . Although the flow is also expected to dominate the high-degree harmonics³, the gravity harmonics beyond J_{10} are still beneath the level of the measurement uncertainty⁵. In addition, because the low-degree even J_n are dominated by solid-body rotation, the only current measurements that can be uniquely related to the dynamics are the low-degree odd harmonics J_3 to J_9 . Therefore, in this study, we use only those to infer the depth of the cloud-level winds.

Because Jupiter is rotating with a short period of 9.92 h, the flow within the planet to leading order is in geostrophic balance, meaning that the momentum budget is dominated by the balance between the Coriolis force and the horizontal pressure gradients. As a consequence,

the flow to leading order is in thermal wind balance, namely

$$2\Omega \cdot \nabla(\rho_s \mathbf{u}) = \nabla \rho' \times \mathbf{g} \quad (1)$$

where Ω is the planetary rotation rate vector, \mathbf{u} is the velocity field, ρ_s and ρ' are the static and dynamic components of the density, respectively, and \mathbf{g} is the gravity obtained by integrating ρ_s (see Methods)¹⁴. Non-spherical effects can play a part in this balance (for example, the deviation of \mathbf{g} from radial symmetry)^{15,16}; however, it has been shown that to leading order equation (1) captures the dynamical balance well^{16,17} (Extended Data Fig. 1). As the gravity harmonics induced by the flow are related to ρ' directly, we can relate the flow field and the gravity spectrum. Thus, given the measured gravitational field, inversion of equation (1) allows us to infer the flow profile that best matches the measurements. For this inversion we use an optimization based on the adjoint method⁹ (see Methods).

The relation between the odd gravity harmonics and the flow is shown in Fig. 2 for a simple model⁶ where the depth of the cloud-level wind is parameterized with a single decay parameter, H . In this scenario, the interior flow is an extension of the cloud-level flow, along the direction of the spin axis owing to angular momentum constraints (see below)^{14,18}, but decaying exponentially in radius with H being the e-folding decay depth^{6,19}. The Juno-measured values (Fig. 2, dashed lines), show that for all four harmonics, independently, the theoretical values⁶ capture the correct sign of the measured harmonics and indicate that the e-folding decay depth of the flow is between 1,000 km and 3,000 km (Fig. 2, grey shading). Inverting the gravity field⁹, taking into consideration the uncertainties of each of the measured harmonics and their cross-correlated uncertainties (the error covariance matrix, see Methods), gives an e-folding decay depth of about 1,500 km. We note, however, that the measured value of J_5 deviates by a factor of about two from the corresponding theoretical value of a single-parameter deep wind profile, suggesting that a more elaborate vertical flow profile than the simple exponential decay is needed to match the data.

Given that the measurements provide four non-zero odd gravity harmonics, a more complex optimization of the vertical and meridional

Table 1 | The Juno-measured and model odd gravity harmonics

Harmonic	Measured	Model without latitudinal variation	Model with latitudinal variation
$J_3 (\times 10^{-8})$	-4.24 ± 0.91	-5.71 ± 1.67	-5.96 ± 2.33
$J_5 (\times 10^{-8})$	-6.89 ± 0.81	-7.73 ± 0.41	-8.00 ± 0.43
$J_7 (\times 10^{-8})$	12.39 ± 1.68	12.77 ± 0.54	12.04 ± 0.70
$J_9 (\times 10^{-8})$	-10.58 ± 4.35	-8.84 ± 0.42	-9.71 ± 0.72

Model results are shown for optimizations with and without variation of flow depth with latitude. The uncertainties are the 3σ uncertainty values. The model uncertainty is calculated by the optimization procedure (Methods). For the middle (right) column the J_n values correspond to the parameter values given in the caption of Fig. 3 (Fig. 4).

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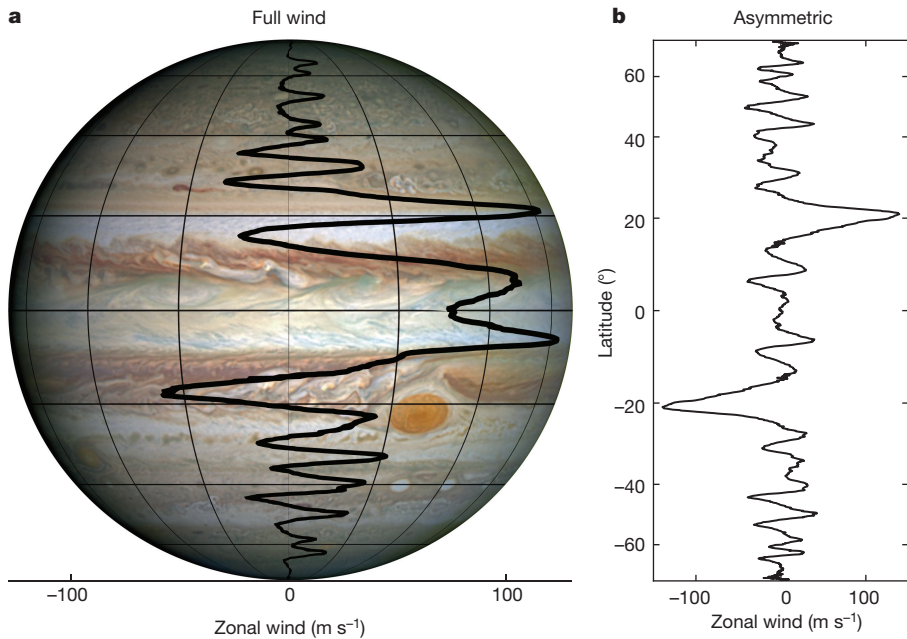


Figure 1 | Jupiter's asymmetric zonal velocity field. **a**, The cloud-level zonal flows (thick black line) as a function of longitude, as measured during Juno's third perijove pass on 11 December 2016 (ref. 30). The image of Jupiter was taken by the Hubble Wide Field Camera in 2014 (<https://en.wikipedia.org/wiki/Jupiter>). Grid latitudes are as in **b** and the longitudinal spread is 45° . Zonal flow scale is the same as the longitudinal grid on the sphere. **b**, The asymmetric component of the flow, taken as the difference between the northern and southern hemisphere cloud-level flows.

profiles of the zonal flow is indeed feasible. Motivated by the Galileo probe measurement of a relatively constant wind profile²⁰ between 4 bar and 22 bar, and magnetohydrodynamic theory suggesting that ohmic dissipation will cause a more abrupt decay of the flow at depth^{7,8,21,22}, we add—in addition to the exponential decay function used in the first estimate (Fig. 2)—a vertical decay profile expressed as a hyperbolic tangent ('tanh') function and a free parameter α , representing the ratio between the two functions. This allows for a much wider range of vertical decay profiles, with three free parameters defining the vertical profile of the flow: the depth H represents the inflection point of the tanh function, ΔH represents the decay width of the tanh function and α is the ratio between the tanh function and an exponential decay with the same decay depth H . Using these three parameters as control parameters in the inverse adjoint model, the optimization process (Fig. 3) minimizes a cost function, taking into account the uncertainties in the gravity measurements, including the error covariance between the different harmonics (Methods)^{9,23}.

Beginning with an assumed vertical decay profile as an initial condition (dashed line in Fig. 3a and black squares in Fig. 3b, c), the optimization iteratively minimizes the cost function, reaching a unique global minimum in the three-dimensional parameter space of H , ΔH and α (red dot in Fig. 3b, c). The best optimized solution, defining a particular vertical profile of the zonal flow (red line in Fig. 3a), is achieved with $H = 1,803 \pm 351$ km, $\Delta H = 1,570 \pm 422$ km and $\alpha = 0.92 \pm 0.26$, where the error is calculated by the optimization process (see Methods), indicating a very deep flow profile containing a large mass. We note that the minimum of the cost function for ΔH is rather flat towards lower ΔH (Fig. 3b), indicating that a flow profile with a much more abrupt decay at depth is compatible with the measured J_n . Integrating the density profile ρ_s down to where the flow decreases noticeably (about 3,000 km) reveals that this region contains about 1% of Jupiter's mass (the mass dependence on depth is shown in Extended Data Fig. 2). This large mass of the dynamical atmosphere (the region that is differentially rotating) is consistent with the persistence of the observed jets over the past several decades². In an accompanying paper¹⁰ we show that, on the basis of the even harmonics, beneath this dynamical atmosphere, in Jupiter's deep interior, there is probably very little zonal flow. The angular momentum of this flow is about 2×10^{-5} that of the solid-body rotating planet.

The solution shown in Fig. 3a (red line) implies that the meridional profile of the flow at depth is strongly correlated with the cloud-level flow. To test the statistical significance of this solution we generate a

large set of synthetic zonal wind profiles (Extended Data Fig. 3) by expanding the observed flow up to high-degree Legendre polynomials and summing them back up while assigning random signs to the expansion coefficients. We find that the solution using the observed cloud-level wind profile (Extended Data Fig. 4, black) is one of the closest solutions to the measurements (Extended Data Fig. 4, red) and only a very small subset of the random flow profiles (less than 1%) give a lower cost-function value (Extended Data Fig. 4, green). This shows that it is statistically improbable that the meridional profile of the flow changes with depth, or that the solution was found by chance (see further discussion in Methods).

Considering the angular momentum budget is helpful for developing a mechanistic understanding of these deep dynamics. Modelling studies

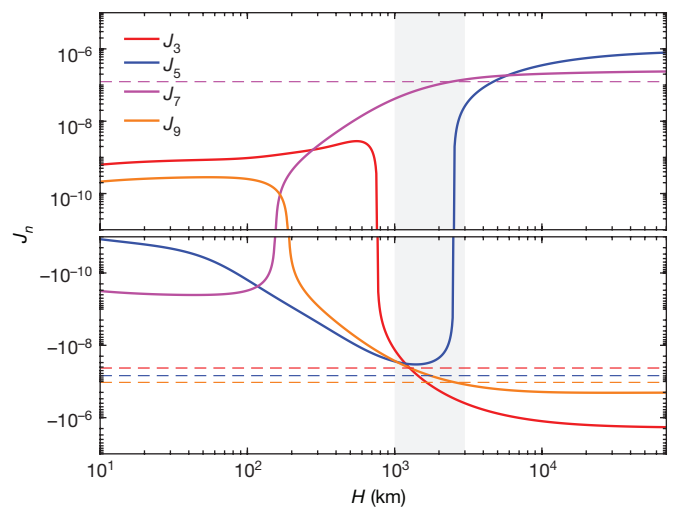


Figure 2 | The odd gravity harmonics as function of a single e-folding decay depth parameter H . The predicted values⁶ (solid) and the Juno-measured values⁵ (dashed, corresponding to the values in Table 1) for J_3 (red), J_5 (blue), J_7 (magenta) and J_9 (orange) are shown as functions of H . All four gravity harmonic measurements, independently, indicate that the e-folding depth of the flow is 1,000–3,000 km (grey shading). All four odd harmonics are small if the flows are shallow, and become large for deeper flows that contain more mass. The change in sign at different decay depths depends on the way the flow pattern projects onto the different Legendre polynomials.

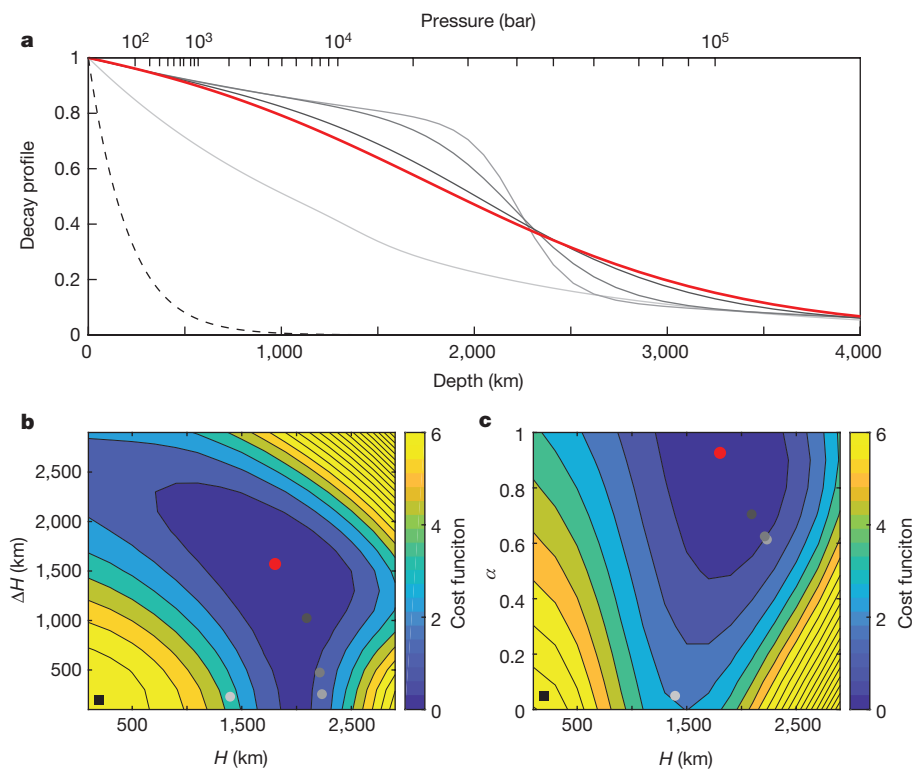


Figure 3 | Jupiter's optimized vertical profile of the zonal wind. **a**, The vertical profile of the flow from the optimization process, beginning with an initial profile (dashed), which evolves along the optimization process (from light to dark shades of grey), leading to the best optimized vertical profile (red), with the parameters $H = 1,803 \pm 351$ km, $\Delta H = 1,570 \pm 422$ km and $\alpha = 0.92 \pm 0.26$ (equation (13) in Methods). The abscissa shows both the depth (bottom) and pressure (top) beneath the 1-bar level. **b**, The cost function in the plane of H and ΔH showing a robust minimum at $H = 1,803$ km and $\Delta H = 1,570$ km (red dot). **c**, The cost function in the plane of H and α showing a minimum at $H = 1,803$ km and $\alpha = 0.92$ (red dot). In **b** and **c** the grey-shaded dots correspond to the grey-shaded curves in **a**. Cost-function values in the colour scale are divided by 1,000 (see calculation in Methods). A statistical significance test for the latitudinal dependence of the flow profile appears in Extended Data Figs 4 and 5.

have suggested^{18,21} that the leading-order angular momentum balance is $\mathbf{u} \cdot \nabla M = D - S$, where \mathbf{u} is the mass-averaged velocity, M is the total angular momentum, D is the drag due to the Lorentz force at depth and $S = (1/\rho) \nabla \cdot (\rho \overline{\mathbf{u}'M'})$ is the eddy angular momentum flux divergence, with the overbar indicating a zonal and temporal mean. At the observed cloud level, the eastward (westward) jets are correlated with regions of eddy momentum flux convergence (divergence), that is, where S is negative (positive)^{21,24}. Below that, where the eddy momentum flux convergence is expected to become weak²⁴, that is, $\mathbf{u} \cdot \nabla M \approx 0$, the flow is along angular momentum surfaces, which on Jupiter are almost entirely parallel to the axis of rotation^{14,18,25}. Then, in the deep region, where the fluid becomes electrically conducting (mainly due to pressure ionization) and the Lorentz force may become important (depending on the magnetic field structure) the leading-order balance is $\mathbf{u} \cdot \nabla M = D$ and the circulation closes. Kinematic dynamo models, which calculate the magnetic drag at depth on the basis of the radially varying electric conductivity inside Jupiter, find that the depth at which the Lorentz drag D becomes important^{7,8} is about 3,000 km. Thus, the theoretical magnetic field considerations and the gravity measurements, which are completely independent, give very consistent results.

Three-dimensional hydrodynamic models of Jupiter, driven by shallow atmospheric turbulence^{21,26} or deep internal convection¹⁴, have found that the low latitudes are often more barotropic than the high latitudes. Thus, an additional level of complexity that can be added to the optimization is allowing the decay depth H to vary with latitude. To limit the number of optimized parameters, the decay depth is expanded in Legendre polynomials to second order, increasing the number of optimized parameters to four (see Methods). Similarly to the case of a latitudinally independent vertical profile (Fig. 3), in this case the optimized vertical decay profile is rather barotropic at lower depths and extends to great depth (Fig. 4a). The optimization uncertainty is shown graphically by the blue shading, with the values for the profile at the equator given in the caption. At higher latitudes, the vertical decay occurs at shallower depths, and the associated uncertainty grows to approximately 500 km (Fig. 4b). The values of J_n corresponding to the solutions of Figs 3 and 4 appear in Table 1. We note that with more free parameters than used in these optimizations, closer matches

to the measurements can be reached. However, the power of these solutions is that they are based on relatively simple extensions of the cloud-level flow, giving results remarkably close to all four independent gravity measurements; and, regardless of the exact vertical profile, the solutions indicate that the observed cloud-level flows extend to depths of thousands of kilometres.

The flow profile determined by the odd harmonics also has a signature in the even harmonics. Owing to the uncertainty in the bulk interior density structure of Jupiter^{10,27}, there is a wide range of solutions for the low-degree static gravity harmonics J_n^s , which does not allow us to test uniquely whether the ΔJ_n from the even harmonics matches the measured values via $\Delta J_n = J_n - J_n^s$. However, for J_8 and J_{10} the interior models are very constraining¹⁰, giving values between -245.7×10^{-8} and -246.3×10^{-8} for J_8^s , and between 20.1×10^{-8} and 20.4×10^{-8} for J_{10}^s (for interior models that also match J_4 and J_6). The measured Juno values are $J_8 = (-242.6 \pm 0.8) \times 10^{-8}$ and $J_{10} = (17.2 \pm 2.3) \times 10^{-8}$, meaning that a positive (negative) correction by the dynamics is needed to match the measurements for J_8 (J_{10}). The values corresponding to the flow profiles presented in Figs 3 and 4 (Extended Data Table 1) are indeed such that for both cases, and for both J_8 and J_{10} , the dynamical corrections can reconcile the differences between the measurements and the internal models, further confirming that the inferred flow profile presented here matches the measurements from Juno. An accompanying paper¹⁰ shows that using the range of current interior models gives further constraints on possible deeper interior flow.

Juno's gravity measurements are consistent with Juno's microwave radiometer measurements, indicating a north-south asymmetry in the sub-cloud-level atmospheric composition, and a direct signature of the main equatorial belt to the maximum depth of the microwave sensitivity^{11,28} at about 1,000 bar. With more Juno orbits the microwave measurements^{4,29} will obtain greater and improved thermal mapping of the deep atmosphere, which will better constrain the water and ammonia abundances as well as the atmospheric flows at those levels. As the Juno mission completes its global mapping of Jupiter, the combination of the gravity, magnetic and microwave data may provide further insights into the coupling between Jupiter's deep interior and atmospheric flows.

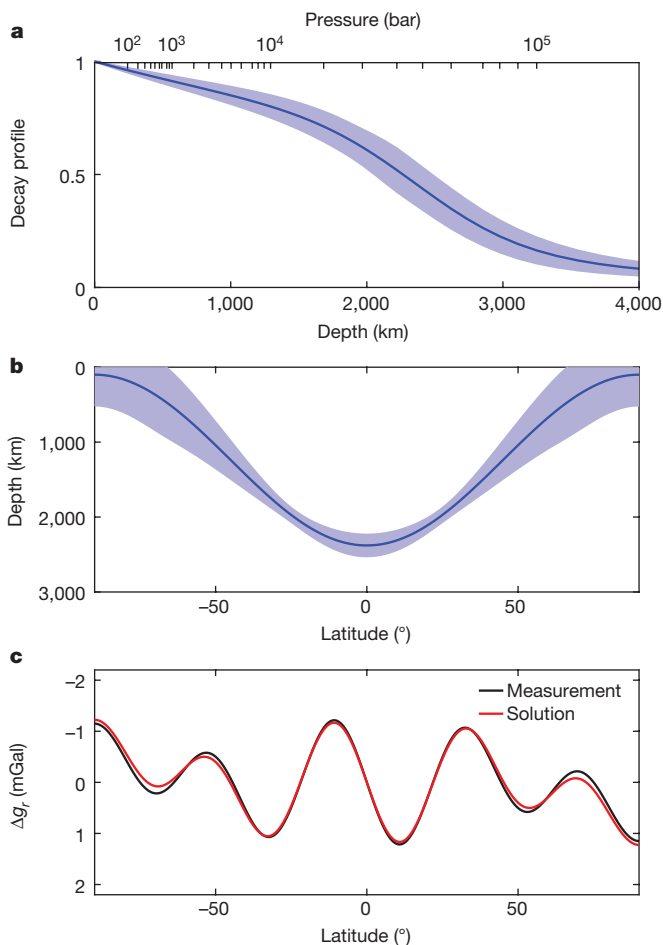


Figure 4 | Jupiter's optimized vertical profile of the zonal wind when allowing for its latitudinal variation. **a**, The vertical profile of the flow at the equator from the optimization process (blue line) and its uncertainty (blue shading). The best optimized values at the equator are $H = 2,379 \pm 142$ km, $\Delta H = 819 \pm 437$ km and $\alpha = 0.62 \pm 0.09$. The abscissa shows both the depth (bottom) and pressure (top) beneath the 1-bar level. **b**, The variation of the inflection point (as shown in **a**) with latitude (blue line) and its uncertainty (blue shading). Details of the latitudinal dependence of H and its functional form are given in Methods (equation (13)). **c**, The Juno measurement of the asymmetric gravity field Δg_l (for J_3 – J_9) as a function of latitude and the corresponding values from the best-fit solution (**a** and **b**), showing a good match between the measurements and the optimized solution (see calculation in Methods).

Online Content Methods, along with any additional Extended Data display items and Source Data, are available in the online version of the paper; references unique to these sections appear only in the online paper.

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Author Contributions Y.K. and E.G. designed the study. Y.K. wrote the paper. E.G. developed the gravity inversion model. D.J.S. led the working group within the Juno Science Team and provided theoretical support. W.B.H. initiated the Juno gravity experiment and provided theoretical support. W.B.H., T.G., Y.M., R.H., B.M. and S.L.W. provided interior models and tested the implications of the results. L.I., D.D., W.M.F. and M.P. carried out the analysis of the Juno gravity data. H.C., D.J.S. and J.B. supported the interpretation regarding the magnetic field. J.I.L. and A.P.I. provided theoretical support. S.J.B., S.M.L. and J.E.P.C. supervised the planning, execution and definition of the Juno gravity experiment. All authors contributed to the discussion and interpretation of the results within the Juno Interiors Working Group.

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METHODS

Calculation of the dynamical gravity harmonics. The gravity harmonics J_n are defined as a weighted integral over the interior density distribution $J_n = -(Ma^n)^{-1} \int P_n \rho r^n d^3r$, where M is the planetary mass, a is the equatorial radius, P_n is the n th Legendre polynomial, ρ is the local density and r is the local radius³¹. On planets with internal dynamics, the density is perturbed by the flow so that the total density in J_n can be written as $\rho = \rho_s + \rho'$, where the density ρ_s is the hydrostatic density resulting from the background rotation and internal density distribution^{27,32–35}, and ρ' are the density fluctuations arising from the atmospheric and internal dynamics¹⁹. The gravity harmonics can be similarly decomposed into two parts $J_n = J_n^s + \Delta J_n$, where the static component J_n^s is due to the planet's internal density distribution and shape^{12,36}, and the dynamical component ΔJ_n is due to the density deviations related to the flow¹⁹.

To develop the relation between the flow on Jupiter and the gravity field measured by Juno, we consider the full momentum balance on a rotating planet

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} + 2\boldsymbol{\Omega} \times \mathbf{u} + \boldsymbol{\Omega} \times \boldsymbol{\Omega} \times \mathbf{r} = -\frac{1}{\rho} \nabla p + \nabla \Phi \quad (2)$$

where \mathbf{u} is the three-dimensional flow vector, $\boldsymbol{\Omega}$ is the planetary rotation rate vector (magnitude, $1.76 \times 10^{-4} \text{ s}^{-1}$), ρ is the density, p is the pressure and Φ is the body force potential set by gravity³⁷ so that $\nabla \Phi = -\mathbf{g}$. The first term on the left-hand side is the local acceleration of the flow, the second is the Eulerian advection, the third is the Coriolis acceleration and the fourth is the centrifugal acceleration. On the right-hand side are the pressure gradient and the body force. Frictional forces are neglected. For Jupiter parameters and large-scale motion, the Rossby number is small, $\text{Ro} \equiv U/\Omega L \approx 0.05$, where U is the typical value of the velocity (100 m s^{-1}) and L is the typical jet scale (10^4 km). The small Rossby number implies that the first two terms are negligible compared to the Coriolis term, so that

$$2\boldsymbol{\Omega} \times (\rho \mathbf{u}) = -\nabla p - \rho \mathbf{g} - \rho \boldsymbol{\Omega} \times \boldsymbol{\Omega} \times \mathbf{r} \quad (3)$$

Because for Jupiter parameters the ratio between the two latter terms on the right-hand side of equation (3) is $a\Omega^2/g \approx 0.1$, and not two orders of magnitude smaller, as it is for Earth parameters, we do not a priori make the traditional approximation merging the centrifugal force with the gravity term³⁸, but solve for the full system, allowing the density, pressure and gravity to be functions of radius r and latitude θ . We separate the solution into a static solution in which $\mathbf{u} = \mathbf{0}$, with the solutions $\rho_s(r, \theta)$, $p_s(r, \theta)$ and $\mathbf{g}_s(r, \theta)$ of the leading-order equation

$$\mathbf{0} = -\nabla p_s - \rho_s \mathbf{g}_s - \rho_s \boldsymbol{\Omega} \times \boldsymbol{\Omega} \times \mathbf{r} \quad (4)$$

and the deviations $\rho'(r, \theta)$, $p'(r, \theta)$ and $\mathbf{g}'(r, \theta)$ due to the dynamics, where $\rho = \rho_s + \rho'$, $p = p_s + p'$ and $\mathbf{g} = \mathbf{g}_s + \mathbf{g}'$. For the static part of the solution we use solutions from interior models^{27,39}. Subtracting equation (4) from equation (3) gives the leading-order dynamical equation

$$2\boldsymbol{\Omega} \times (\rho_s \mathbf{u}) = -\nabla p' - \rho_s \mathbf{g}' - \rho' \mathbf{g}_s - \rho' \boldsymbol{\Omega} \times \boldsymbol{\Omega} \times \mathbf{r} \quad (5)$$

Taking the curl of equation (5), eliminating the dependence on pressure, yields a single equation in the azimuthal direction

$$\begin{aligned} -2\Omega r \partial_z (\rho_s u) = & -r g_s^{(\theta)} \frac{\partial \rho'}{\partial r} - g_s^{(r)} \frac{\partial \rho'}{\partial \theta} + r \frac{\partial \rho_s}{\partial r} g^{(\theta)} - g^{(r)} \frac{\partial \rho_s}{\partial \theta} \\ & - \Omega^2 r \left[\frac{\partial \rho'}{\partial \theta} \cos^2 \theta + \frac{\partial \rho'}{\partial r} r \cos \theta \sin \theta \right] \end{aligned} \quad (6)$$

where u is the velocity component in the azimuthal direction, the superscripts (r) and (θ) denote the radial and latitudinal components, respectively, and the notation $\partial_z \equiv \cos \theta \frac{\partial}{\partial r} + \sin \theta \frac{\partial}{\partial \theta}$ denotes the derivative along the direction of the axis of rotation. Note that this is an integro-differential equation because the gravity \mathbf{g}' is calculated by integrating ρ' . Although this equation can be solved numerically¹⁷, it is very difficult to solve at the required resolution and the approximation below is sufficient for relating the flow field and the gravity harmonics¹⁷.

A typical solution to equation (6), corresponding to the flow field in Fig. 3, is given in Extended Data Fig. 1. It shows that the leading-order balance is between the left-hand-side term and the second term on the right-hand side of equation (6). All other terms are at least an order of magnitude smaller, and have a very small contribution to the gravitational harmonics¹⁷. Thus, by taking $\mathbf{g} = \mathbf{g}_s(r)$ in equation (3) and neglecting the centrifugal term gives the leading-order solution. The curl of equation (3) then gives the leading-order equation—equation (1)—which is a generalized form of the thermal wind equation^{14,19}. We note that if a higher correction is desired, all terms in equation (6) must be maintained because the smaller terms in equation (6) partially cancel each other (Extended Data Fig. 1). Approximations not maintaining all these terms would be invalid¹⁵.

The zonal component of equation (1) is then

$$2\Omega r \partial_z (\rho_s u) = g_s^{(r)} \frac{\partial \rho'}{\partial \theta} \quad (7)$$

which can be integrated to find a solution for the dynamical part of the density given by

$$\rho'(r, \theta) = \frac{2\Omega r}{g_s} \int_{-\pi/2}^{\pi/2} \partial_z (\rho_s(r) u(r, \theta')) d\theta' + \rho'_0(r) \quad (8)$$

where $\rho'_0(r)$ is an unknown integration function that depends only on radius. Although the density ρ' cannot be determined uniquely owing to the unknown $\rho'_0(r)$, the gravity harmonics due to dynamics

$$\Delta J_n = -\frac{2\pi}{Ma^n} \int_{-\pi/2}^{\pi/2} \cos \theta d\theta \int_0^a r^{n+2} P_n(\sin \theta) \rho'(r, \theta) dr \quad (9)$$

can be determined uniquely since

$$\int_{-\pi/2}^{\pi/2} \cos \theta d\theta \int_0^a r^{n+2} P_n(\sin \theta) \rho'_0(r) dr = 0 \quad (10)$$

To avoid integrating over discontinuities at the equator the integration is performed from the equator poleward in both hemispheres separately⁴⁰. Therefore, given any flow profile, the anomalous density gradient can be determined to leading order (equation (8)) and the resulting dynamical gravity harmonics can be calculated (equation (9)). We note that the sphericity assumption leaves the choice of using the equatorial radius or the mean radius for a . For consistency with the standard normalization^{5,41} of J_n we use the equatorial radius, but repeating the calculation with the mean radius gives results within one per cent of those presented here.

Calculation of the gravity anomaly. Equivalent to the gravity harmonics is the physical gravity anomaly (Fig. 4c), which emphasizes the nature of the solution as function of latitude¹⁹. The gravity anomaly in the radial direction on the surface of a planet that results from the asymmetric flow is given by

$$\Delta g_r(\theta) = -\frac{GM}{a^2} \sum_n (n+1) \Delta J_n P_n(\sin \theta) \quad (11)$$

where G is the gravitational constant and $n = 3, 5, 7$ and 9 . In Fig. 4c we show a comparison between the measured⁵ and the calculated gravity anomalies. The better match at low latitudes is a result of the measurements having smaller uncertainties at low latitudes owing to the trajectory of the spacecraft, which is at periaapses near Jupiter's lower latitudes during the initial phase of the Juno mission^{11,41}.

Setup of the flow structure. Our knowledge of the flow field of Jupiter so far comes almost completely from cloud tracking^{30,42}. We use this flow field as an upper boundary, and extend the flow into the interior by optimizing the general functions below. Angular momentum constraints require that the flow into the interior follows angular momentum surfaces^{14,18,25} (see main text), which on Jupiter are nearly parallel to the direction of the axis of rotation. Magnetic drag⁷ and the compressibility of the fluid¹⁴ require that the flow decays at some depth, and therefore we use a flow field with the following general structure

$$u(r, \theta) = u_{\text{cyl}}(s) Q(r) \quad (12)$$

where $u_{\text{cyl}}(s)$ is the cloud-level azimuthal wind projected downward along the direction of the axis of rotation, and $s = r \cos(\theta)$ is the distance from the axis of rotation. $Q(r)$ is the radial decay function we optimize, given by

$$Q(r) = (1 - \alpha) \exp\left(\frac{r-a}{H(\theta)}\right) + \alpha \left[\frac{\tanh\left(\frac{-a-H(\theta)-r}{\Delta H}\right) + 1}{\tanh\left(\frac{H(\theta)}{\Delta H}\right) + 1} \right] \quad (13)$$

where a is the planetary radius, α is the contribution ratio between an exponential and a normalized hyperbolic tangent function and ΔH is the width of the hyperbolic tangent. We take a hierarchical approach using this profile at several levels of complexity. First, setting $\alpha = 0$, the flow is parameterized as a simple exponential decay, with H being independent of latitude, as has been done in many previous studies^{6,10,19,43,44}. Then, allowing $0 < \alpha < 1$, the flow is parameterized (Fig. 3), with three free parameters— α , H and ΔH —as they appear in equation (13), but still keeping H as a single number. As a final step (Fig. 4), H is allowed to vary as a function of latitude and defined as

$$H(\theta) = H_0 + H_2 P_2(\sin\theta) \quad (14)$$

where H_0 is the single latitude-independent depth used in the first and second setups, and H_2 is the additional parameter used to set the amplitude of the latitude-dependent second Legendre polynomial function P_2 . For the optimization shown in Fig. 4 the values are $H_0 = 1,619 \pm 150$ km and $H_2 = -1,519 \pm 459$ km. We note that the hyperbolic function is normalized by its value at the surface of the planet to ensure that the surface flow has the value of the measured cloud-level wind. Expansion of $H(\theta)$ to higher harmonics is possible, but additional optimized parameters increase the solution uncertainty (see below), and therefore we restrict this expansion only to second order.

The optimization procedure. The methodology described here is similar to that used in ref. 23. We find the values of a set of control variables that makes the model solution for the gravity harmonics as close as possible to the measured gravity harmonics. The number of optimized control variables in the three setups varies between one and four parameters, as discussed above. The measure for the desired proximity of the model solution to the measurements (a cost function) takes into account our knowledge regarding the observational errors. The optimization procedure provides an efficient way to reach the global minimum of the cost function.

Since α has different units from those of H and ΔH , the problem is best conditioned when the total control vector is composed from the different parameters normalized by their typical values. We define the general control vector as

$$\mathbf{X}_C = (H_0/h_{\text{nor}}, \Delta H/h_{\text{nor}}, \alpha/\alpha_{\text{nor}}, H_2/h_{\text{nor}})^T \quad (15)$$

where $h_{\text{nor}} = 10^7$ m and $\alpha_{\text{nor}} = 1$. In the optimization procedure, the values of the normalized control variables H_0/h_{nor} , $\alpha/\alpha_{\text{nor}}$ and $\Delta H/h_{\text{nor}}$ are limited to the range of 0 to 1, and the value of H_2/h_{nor} between -1 and 1 .

The cost function is defined as the weighted difference between the model-calculated odd harmonics and those measured by Juno. Together with an additional penalty term to ensure that the initial guess does not affect the solution, the cost function is

$$L = (\mathbf{J}^m - \mathbf{J}^o)^T W (\mathbf{J}^m - \mathbf{J}^o) + \varepsilon \mathbf{X}_C^T \mathbf{X}_C \quad (16)$$

where $\mathbf{J}^m = (J_3^m, J_5^m, J_7^m, J_9^m)^T$ is the calculated model solution, $\mathbf{J}^o = (J_3^o, J_5^o, J_7^o, J_9^o)^T$ is the measured one, and W is the 4×4 weight matrix (Extended Data Table 2), calculated as the inverse of the covariance matrix multiplied by 9 (equivalent to three times the uncertainties). The diagonal terms give the weight assigned to each harmonic independently, and the off-diagonal terms give the weights resulting for the cross-correlation of the measurement errors. The larger the value, the more weight is given in the cost function. For example, looking at the diagonal terms, the largest weight is given to J_5 and the smallest one to J_9 . Importantly, the off-diagonal terms have values that are as large as the diagonal terms, that is, there is a strong correlation between the measurement errors, and therefore we can expect the discrepancy between the model harmonics and the measured ones also to be cross-correlated in the same manner. The second term in equation (16) acts as a penalty term (also known as 'regularization') whose purpose in this case is to ensure that the optimized solution is not affected by the initial guess, or any part of the control vector that does not affect the difference between the calculated and observed gravity harmonics. An extensive discussion of this issue (also known as the null space of the solution) can be found in previous studies^{17,23}. The value of the parameter ε is set according to the initial value of the cost function, so it affects the solution only when the cost function is considerably reduced. The form of the penalty term is set to penalize any non-zero value of the control variable \mathbf{X}_C since there is no prior knowledge of the depth of the flow. Given an initial guess for \mathbf{X}_C , a minimal value of L is searched for using the Matlab function 'fmincon' and taking advantage of the cost-function gradient that is calculated with the adjoint of the dynamical model⁹.

Calculating the uncertainties in the solution. The control variable uncertainties are derived from the Hessian matrix G (second derivative of the cost function L with respect to the control vector \mathbf{X}_C)⁹. For example, in the third setup of the optimization there are 4 parameters that are optimized, therefore the size of the Hessian matrix will be 4×4 . Inverting the Hessian matrix G , we get the solution error covariance matrix C . This matrix includes the error covariance associated with combination of each two control variables (off-diagonal terms), and the variance of each one (diagonal terms). Physically, the covariance matrix indicates the formal uncertainties in the control variables given the uncertainties of the observations (weights W in the cost function). The larger the uncertainties in the observations, the smaller are the weights in the cost-function, and the larger the uncertainties in the control variables. The uncertainties appearing in this study for H , ΔH and α are the square roots of the diagonal terms in the matrix C . We note that in all cases analysed in this work, the off-diagonal terms in C have the

same order of magnitude as the diagonal terms, meaning that uncertainties in the control variable are highly correlated.

Using the uncertainties in the control variable, we can calculate the uncertainties in the model solution for J_n . Since the uncertainties for H , ΔH , and α represent the first standard deviation of the errors, we can statistically estimate the associated error in the J_n values by solving the model with the parameters randomly perturbed around their optimized value (with the perturbations having a normal distribution with the calculated standard deviation). In this study we generate 1,000 such cases, calculate the J_n for each case, and then calculate the standard deviation for each J_n . This is the error value given to each gravity harmonic in Table 1 and Extended Data Table 1.

Statistical significance test for the latitudinal profile. One of the conclusions of this study is that the observed cloud-level meridional profile of the zonal wind, as observed at the cloud-level, extends deep into the interior. This is a strong constraint on the flow, and we investigate its statistical significance here. Since we are optimizing a solution with only four measurements, there exists a possibility that the match obtained with the gravity measurements is by chance and not because the same meridional profile extends to great depths. To exclude this possibility, we examine whether a match with the gravity measurements could be obtained when using a meridional profile different from that of the cloud-level flows. To make a sensible test, the artificial wind profile we examine should have similar characteristics, such as the typical latitudinal width of the jets and their amplitude. To accomplish this, the observed cloud-level wind is decomposed into the first 100 Legendre polynomials

$$U_{\text{surf}}(\theta) = \sum_{i=0}^{99} A_i P_i(\sin\theta) \quad (17)$$

where A_i are the coefficients of the Legendre polynomials. To create the different artificial wind possibilities, the wind is then reconstructed as

$$U_{\text{rand}}^j(\theta) = \sum_{i=0}^{99} S_i^j A_i P_i(\sin\theta) \quad (18)$$

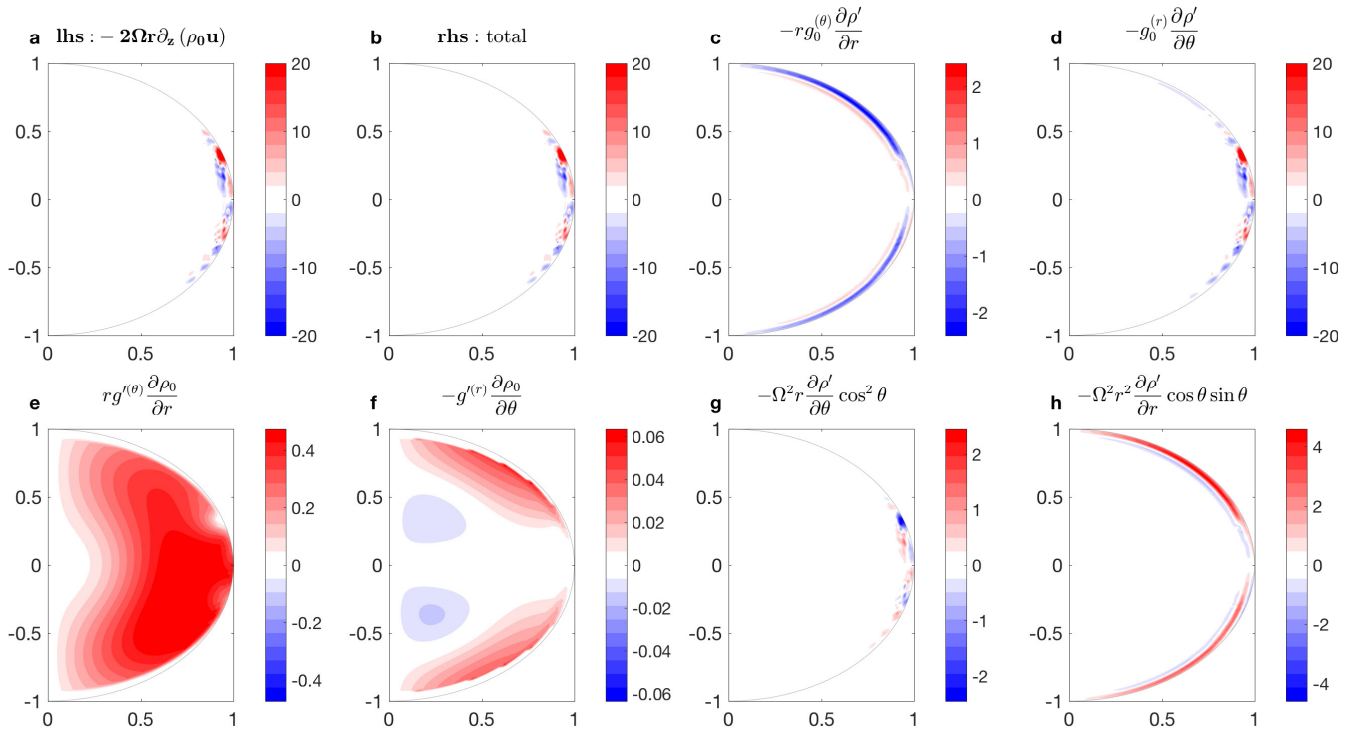
where S_i^j are a 100 plus or minus signs randomly chosen for each realization j of the wind. The resulting artificial cloud-level wind retains the basic characteristics (width and strength) of the observed zonal jets, but their latitudinal locations are now very different. To statistically examine our ability to reach a solution that gives a good match between the model-calculated gravity harmonics and those measured, we generated 1,000 artificial cloud-level wind profiles. A few examples of such randomly generated winds are shown in Extended Data Fig. 3. We note that while the wind profiles are very different from one another, the main characteristics of the observed winds are retained. Extended Data Fig. 4 shows the resulting J_3 , J_5 , J_7 and J_9 for these flow profiles (blue dots), optimized in the same way that the cloud-level wind solutions are. The results indicate that the gravity harmonics calculated using the specific cloud-level wind profile (black points with their uncertainty ellipse), give results closer to the measurements (red points with their uncertainty ellipse) than 99% of the random profiles, indicating the robustness of this result. We note the tendency of the optimized solutions to be in the quarter of the phase space where the measurements are (Extended Data Fig. 4), particularly for the case of J_5 and J_7 , because for these harmonics the absolute value of the measurement is largest and the relative measurement error is smallest (see Table 1), so their weight in the cost function is the largest. Taking the same random set of meridional profiles and calculating their gravity harmonics for a fixed vertical profile (without the optimization process) gives solutions spread equally over all quarters of the parameter space (Extended Data Fig. 5). This illustrates that the tendency of the simple exponential decay solution to have the correct sign and magnitude (Fig. 2) is also very likely not by chance. As an additional test we calculate the solution taking the Jupiter observed cloud-level meridional profile, but extended into the interior radially instead of along the direction of the spin axis. In this case even the sign of the gravity harmonics differs from the measurements. **Non-uniqueness of the gravity inversion.** It is important to note that the gravity inversion problem is non-unique, and as demonstrated in Figs. 3 and 4, different profiles can give similar gravity signatures. In addition, the cases presented here do not match the measurements perfectly, and with more free parameters and/or other meridional profiles⁴⁵ one could achieve better matches to the measurements. However, since the problem is non-unique, achieving a perfect match is not necessarily meaningful. Thus, the rationale of this study is to show that a minimal set of assumptions about the vertical and meridional structure gives by itself a very good, statistically significant, match to the measurements, indicating the structure and extent of the flow. Regardless of the exact vertical profile (which can depend on the parameterization and the non-uniqueness) the gravity measurements robustly reveal that the east-west jet streams on Jupiter are very deep, reaching several

thousands of kilometres beneath the cloud-level (several tens of kilobars of pressure), and advect a large mass that is on the order of one per cent of the mass of the planet.

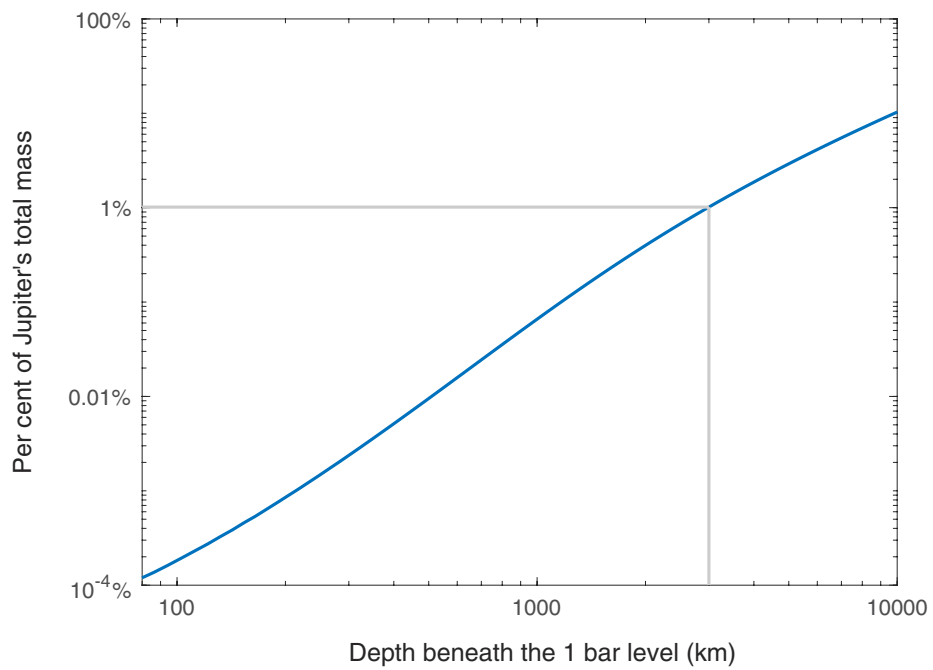
Code availability. The code for inversion of the gravity measurements is available at http://www.weizmann.ac.il/eserpages/kaspi/juno_code/.

Data availability. Figure data are available upon request.

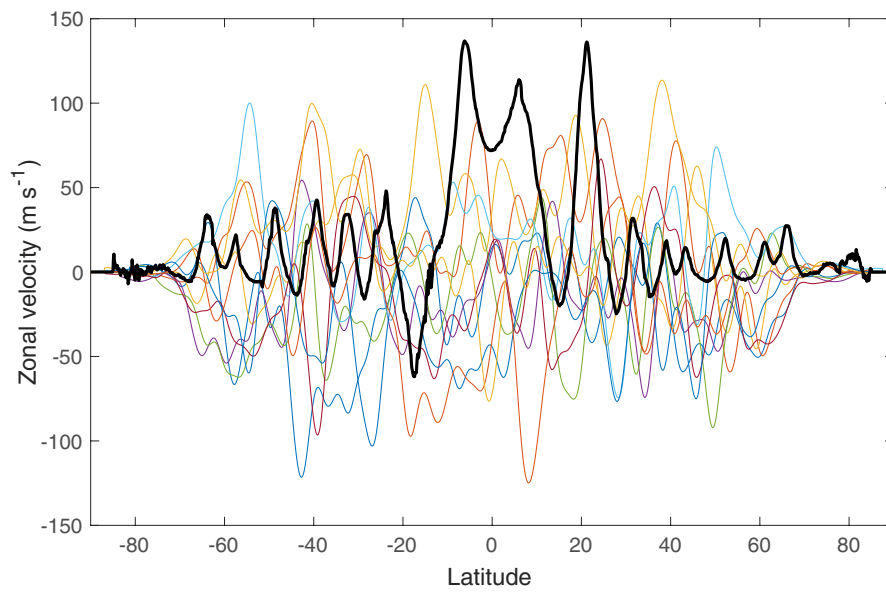
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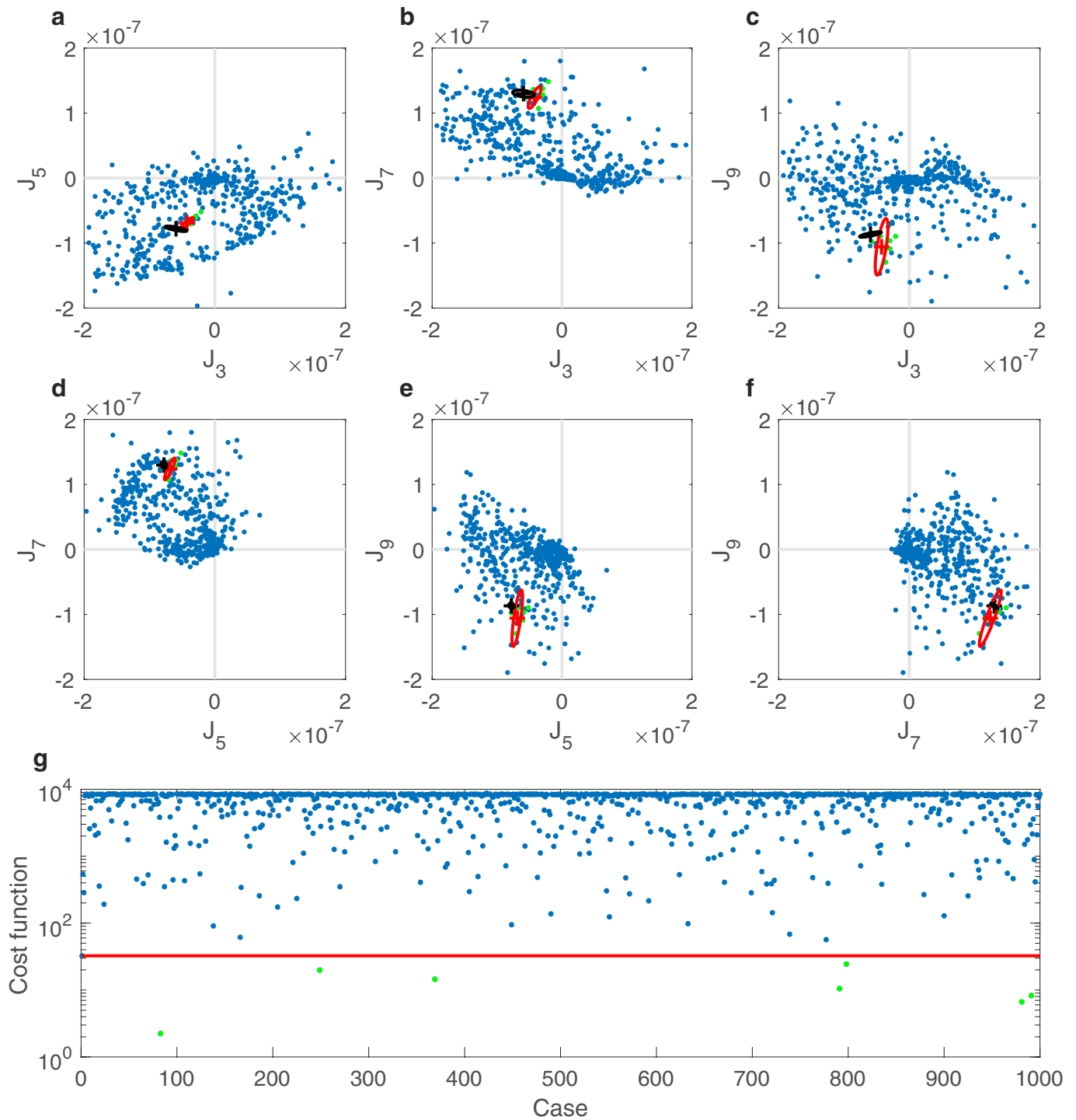
Extended Data Figure 1 | The vorticity balance. Solution to equation (6). **a**, Left-hand-side term with the wind profile from Fig. 3. **b**, Total of the right-hand side. **c–h**, The six terms on the right-hand side of equation (6), showing that the thermal wind balance (**a** and **d**) is the leading-order balance. Note that the different panels have different colour scales.



Extended Data Figure 2 | Jupiter's mass distribution. The percentage of Jupiter's mass as a function of depth beneath the 1-bar level. The grey line shows that roughly 1% of the mass is contained above a depth of 3,000 km.

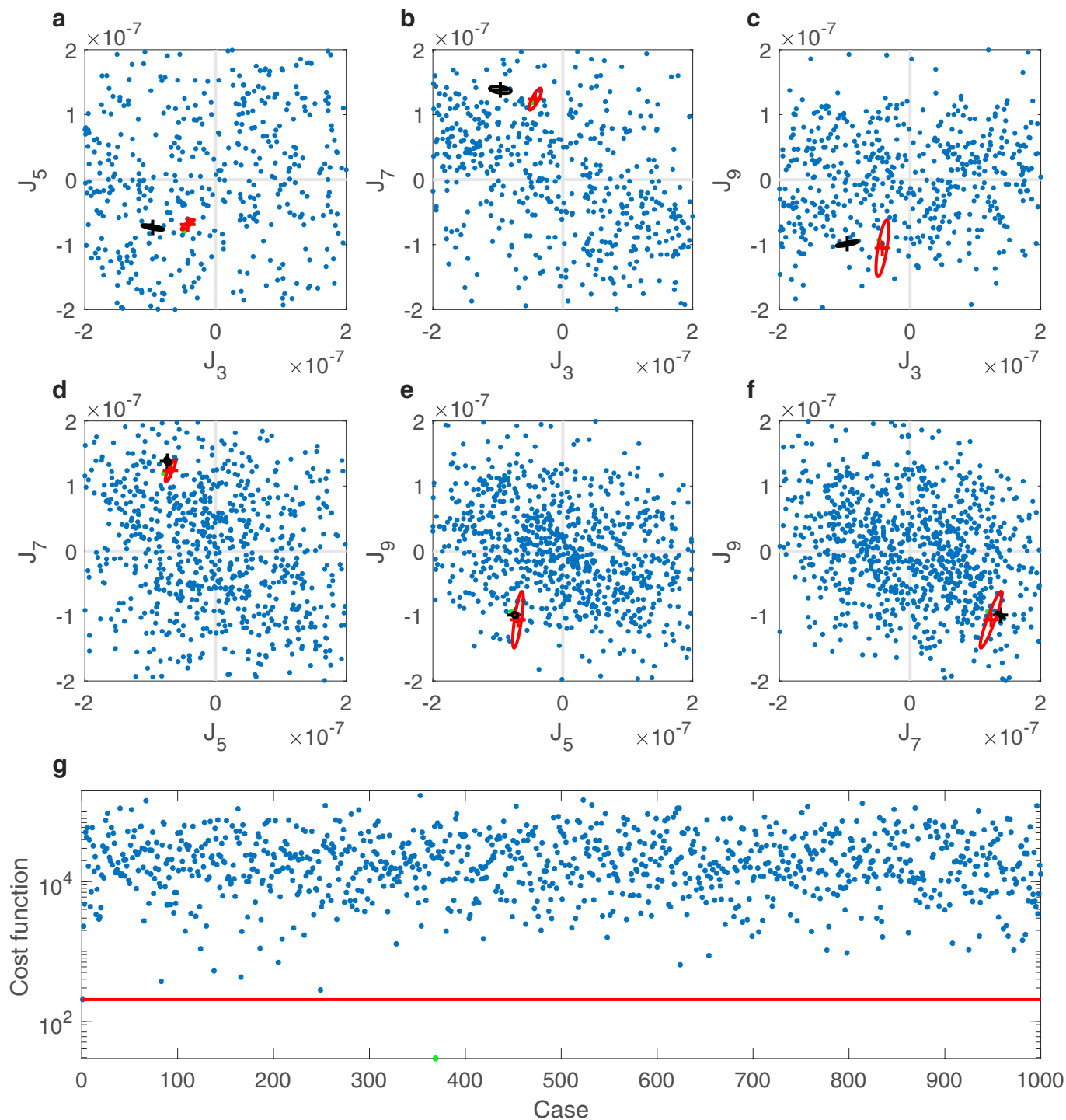


Extended Data Figure 3 | Example of wind profiles used for the statistical significance test. The observed cloud-level wind (black), together with a sample of ten randomly generated wind profiles.



Extended Data Figure 4 | Optimized solutions for the odd harmonics using random zonal wind profiles. a–f, Optimized solutions (blue) for J_3 , J_5 , J_7 and J_9 for flows with 1,000 different artificial meridional profiles of the zonal wind (as in Extended Data Fig. 3). The Juno measurements are shown in red with their corresponding uncertainty ellipse. The optimized solution corresponding to Jupiter’s observed

cloud-level zonal wind profile (Fig. 3) is shown in black with the corresponding uncertainty ellipse. g, The cost function for all different meridional profiles explored, with the red line corresponding to the solution with the Jupiter zonal wind profile. Fewer than 1% of the solutions have lower cost functions (green).



Extended Data Figure 5 | Solutions for the odd harmonics using random zonal wind profiles and a fixed vertical profile. a–f, Solutions (blue) for J_3 , J_5 , J_7 and J_9 for flows with 1,000 different artificial meridional profiles of the zonal wind (as in Extended Data Fig. 3), and the vertical profile held fixed with $H = 2,000$ km, $\Delta H = 1,500$ km and $\alpha = 1$. The Juno measurements are shown in red with their corresponding uncertainty ellipse. The solution with these parameters and using Jupiter's observed cloud-level zonal wind profile is shown in black with the corresponding

uncertainty ellipse. g, The cost function for all different meridional profiles explored, with the red line corresponding to the solution with the Jupiter zonal wind profile. This shows that when no optimization is done (which takes into consideration the relative measurement error of the different harmonics), the solutions are spread equally over all four quadrants in these phase spaces (unlike in Extended Data Fig. 4). Only one solution has a lower cost function (green).

Extended Data Table 1 | Flow-induced even gravity harmonics

$\times 10^{-8}$	Model without latitudinal variation	Model with latitudinal variation
ΔJ_2	54.62 ± 5.21	-48.87 ± 7.93
ΔJ_4	-5.18 ± 0.74	-15.01 ± 7.56
ΔJ_6	0.33 ± 0.35	0.29 ± 1.49
ΔJ_8	5.41 ± 0.28	4.76 ± 0.61
ΔJ_{10}	-5.35 ± 0.25	-4.94 ± 0.71

The even gravity harmonics solutions for the optimization, with and without variation of flow depth with latitude, that correspond to the solutions presented in Figs 3 and 4 and Table 1. The uncertainties are the 3σ uncertainty values.

Extended Data Table 2 | The weights matrix W used in the cost function L of equation (16)

	J_3	J_5	J_7	J_9
J_3	8.32	-11.05	1.45	-0.41
J_5	-11.05	20.21	-12.26	3.35
J_7	1.45	-12.26	14.31	-7.63
J_9	-0.41	3.35	-7.63	7.91

Shown are the weights associated with J_3 , J_5 , J_7 and J_9 (diagonal terms) and those associated with the correlation between the harmonics (off-diagonal terms). The values reflect the uncertainties in the measurements, calculated taking the inverse of the measurement error covariance matrix multiplied by 9 (to reflect 3σ uncertainties). The larger the value, the larger the weight given to it when minimizing the cost function. Values shown are multiplied by 10^{-16} .