

# Line activity of hybrid lipids: stabilization of membrane rafts?

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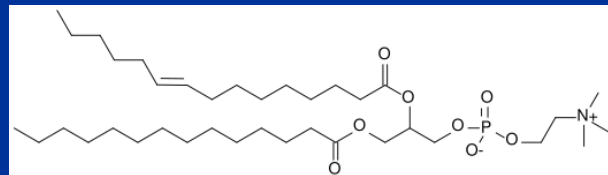
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Hybrid lipids



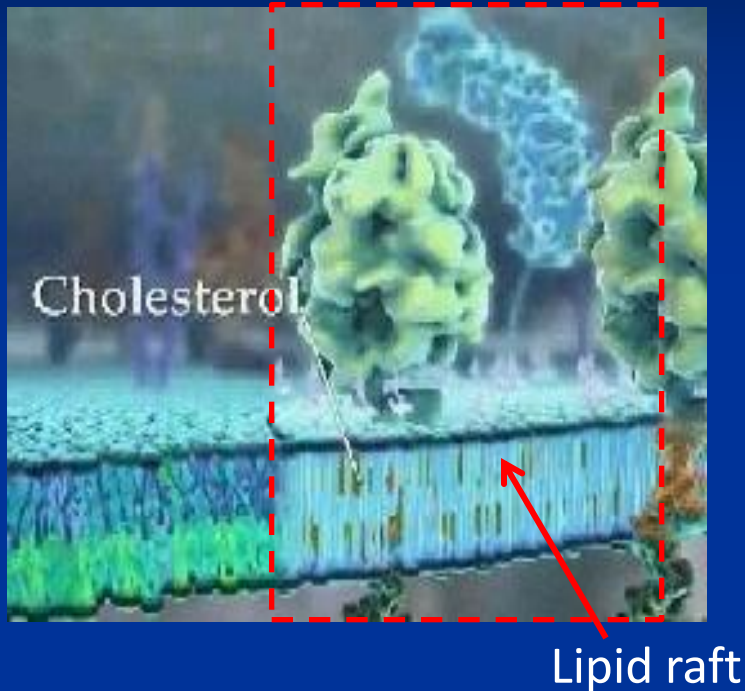
Unsaturated tail



POPC

Saturated tail

# Lipid raft hypothesis – biological systems

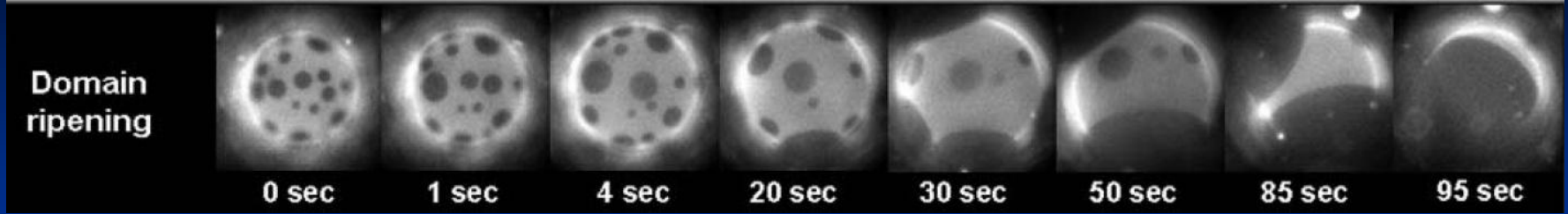


*Lipid raft : small domains in biological membranes – controversial !*

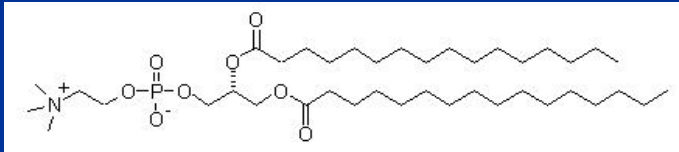
- Rich in saturated lipids
- Metastable or even stable
- The size of the domain is of the linear order of **10 – 100** nm.

(From: *The Inner Life of the Cell*  
[http://multimedia.mcb.harvard.edu/anim\\_innerlife.html](http://multimedia.mcb.harvard.edu/anim_innerlife.html))

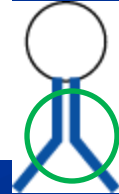
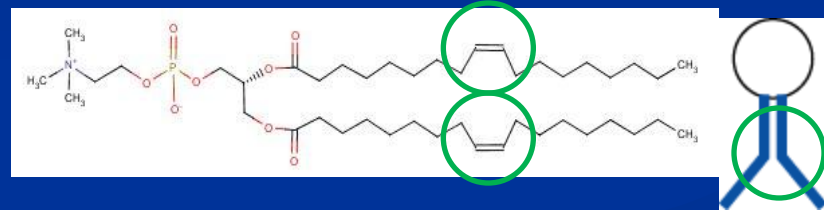
## Domains in lipid vesicles – DPCC, DOPC



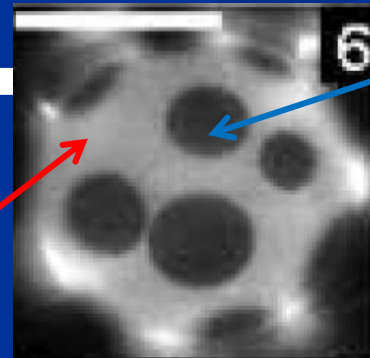
Saturated lipids, *e.g.* DPPC, 



## Unsaturated lipids, e.g., DOPC



20  $\mu\text{m}$



$L_o$  phase: Rich in **S** and the lipid chains are ordered.

$L_d$  phase: Rich in **U** and lipid chains are disordered.

*Veatch and Keller, BPJ, 85, 3074 (2003).*

*Silva et al., submitted.*

# Phase separation: macroscopic or finite domains in lipid mixtures

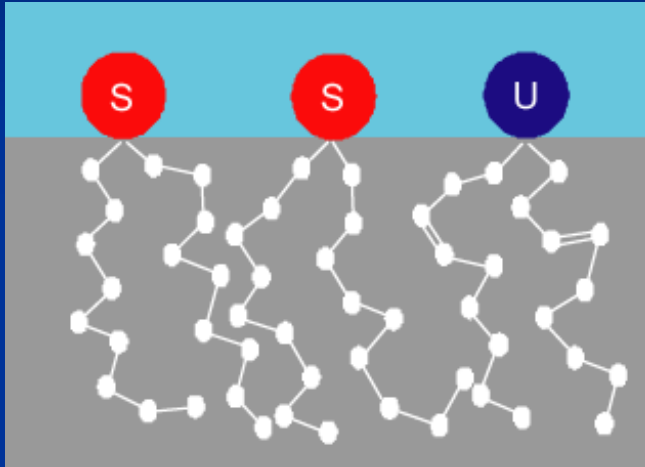
- Phase separation implies positive line tension: separate into macroscopic domains
- How can finite domains be stable (in equilibrium)?
- Line active species reduces interfacial free energy: line analogy of surfactants
- Here, “lineactant\*” chains match the two phases: only chain packing needed to explain effect

\*lineactant:

D. Schwartz, PRL 2008

# Chain packing theory of macroscopic phase separation

Chain packing “frustration” of saturated/unsaturated lipids is the driving force of phase separation of lipid membrane



- Phenomenological potential chain order
- Packing entropy
- Incompressibility of hydrophobic core

# Line activity of hybrid lipid: reduces packing frustration

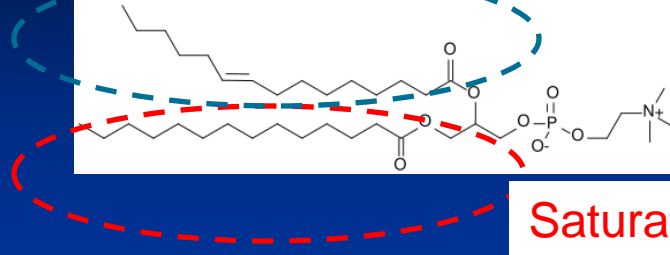
Hybrid lipids



Unsaturated tail

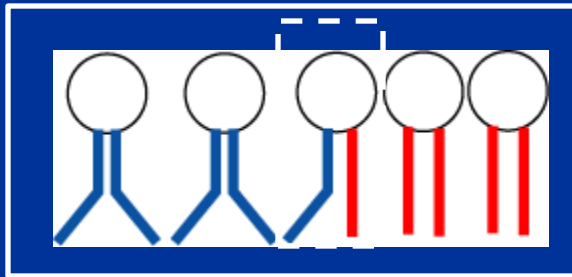
POPC

Biologically abundant

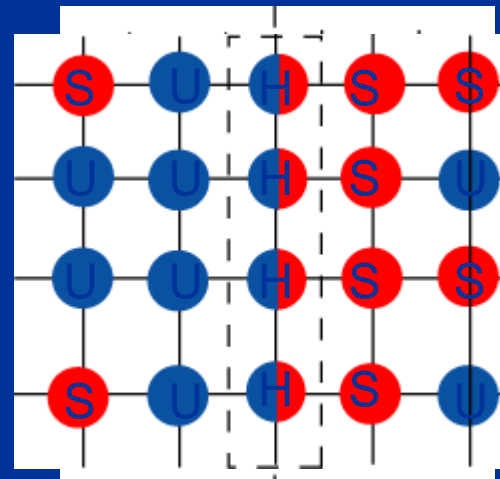


Saturated tail

Side view



Top view

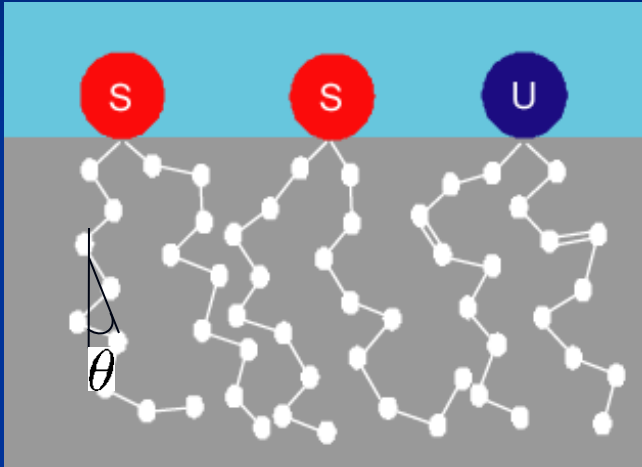


Line tension is reduced to zero for strong interaction (or low temperature).

*R. Brewster, P. A. Pincus, and S. A. Safran, Biophys. J., 97, 1087 (2009)  
and R. Brewster, S. A. Safran, Biophys. J. Lett., in press.*

# Objective

What is role of chain ordering in line activity of  ?



Liquid crystal order parameter

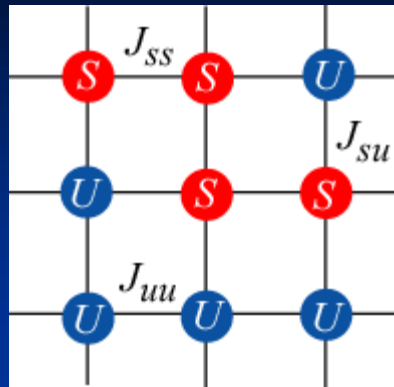
$$S = \left\langle \frac{3 \cos^2 \theta - 1}{2} \right\rangle \quad -0.5 \leq S \leq 1$$

$\theta$ : The angle between the bilayer normal and chain segment

Liquid crystal model to analyze how chain ordering drives phase separation and line activity of hybrid lipids

# Lattice model for membrane without hybrid lipids

Lipids



Assumption:

The order parameter for **U** is  $\sim 0$ ,  
( $S_u \sim 0$ ), because entropy  $\gg$  interaction.

Mixing entropy

$\psi(\mathbf{r})$ : Local concentration of **S**

$$G_{\text{mix}} = k_B T [\psi(\mathbf{r}) \ln \psi(\mathbf{r}) + (1 - \psi(\mathbf{r})) \ln(1 - \psi(\mathbf{r}))]$$

Interaction energy

**(favorable when neighboring chains are ordered - only interactions due to chain ordering)**

$$G_{\text{int}} = -\frac{1}{2} J_{ss} \psi^2(\mathbf{r}) \overline{S_s^2(\mathbf{r})}$$

$S_s(\mathbf{r})$ : Chain order parameter for **S**

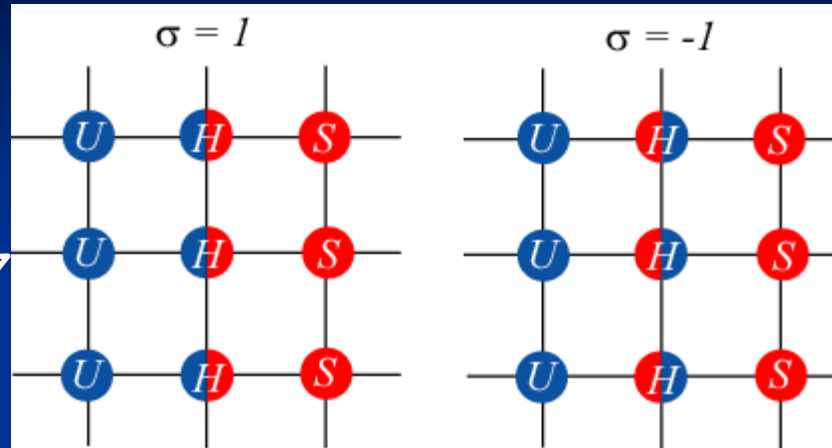
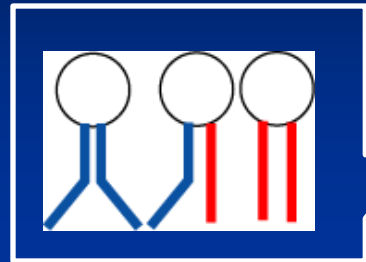
Entropy loss due to chain ordering

$$G_{\text{conf}} = 2k_B T [u_s S_s^4 - w_s S_s^3 + r_{0s} S_s^2] \psi(\mathbf{r})$$

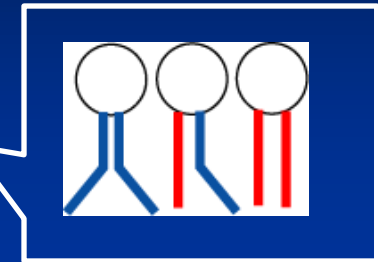
*P. G. de Gennes and J. Prost, The Physics of Liquid Crystals*



# Lattice model for membrane with



$\sigma(\mathbf{r})$ : Orientation of 



Orientation **dependent** part of the interaction energy

$$-\frac{1}{2}J_{ss}S_s(\mathbf{r})\psi_h(\mathbf{r})\sigma(\mathbf{r})\nabla(S_s(\mathbf{r})\psi(\mathbf{r}))$$

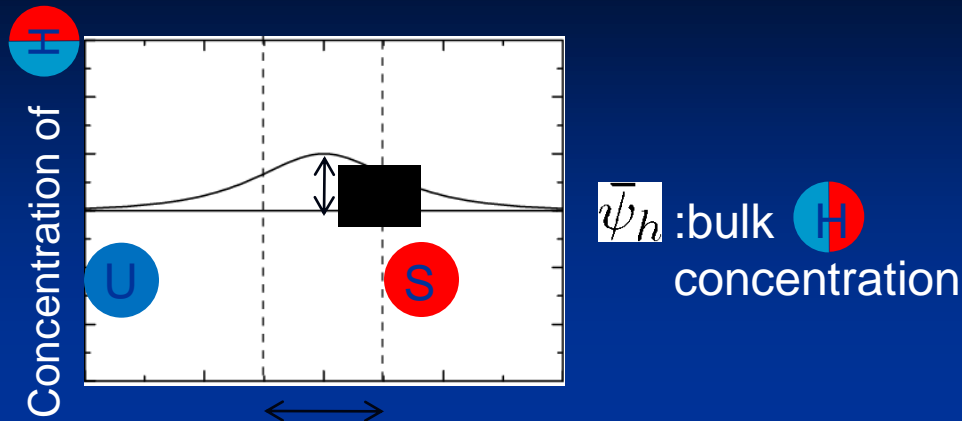
$\psi_h(\mathbf{r})$ :

Local composition of 

Orientational entropy

$$k_B T \left[ \frac{1 + \sigma(\mathbf{r})}{2} \ln \frac{1 + \sigma(\mathbf{r})}{2} + \frac{1 - \sigma(\mathbf{r})}{2} \ln \frac{1 - \sigma(\mathbf{r})}{2} \right] \psi_h(\mathbf{r}).$$

# Weak interaction (high temperature)



Line tension

$$\lambda = \lambda_0 \sqrt{1 - \alpha \psi_h^{\text{int}}} \quad \alpha > 0$$

$\lambda_0$  : Line tension for S + U system with no hybrid

However, concentration of H adsorbed at interfaces is not enough to reduce the line tension to zero near critical point.

# Strong interaction (low temperature)

## Line tension

$$\psi_h^{\text{int}} \rightarrow 1$$

Width of interface  $\xi \sim$  Molecular size

$$\sigma \rightarrow 1$$

Complete orientation

$$\lambda \sim -\frac{1}{2}J_{ss}S_{\text{int}} - k_B T \ln \bar{\psi}_h$$
$$> 0$$

$$\bar{\psi}_h$$

Average of  in the bulk.

$$S_{\text{int}}$$

Chain order parameter of hybrid at the interface  $\sim 1$

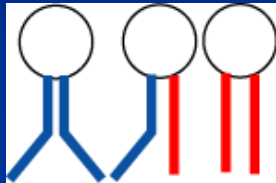
- Line tension is reduced to 0 with decreasing temperature
- Loss of mixing entropy limits this effect to low temperatures

- Interfaces between domains stabilized by hybrid!

- What is the stable size of the domains?

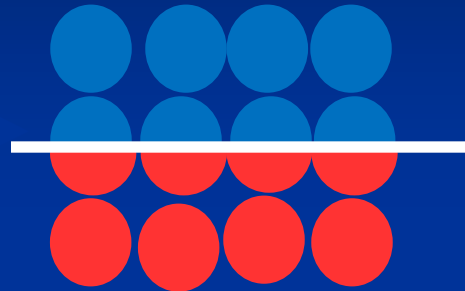
# Domain size: 2D spontaneous curvature

Side view



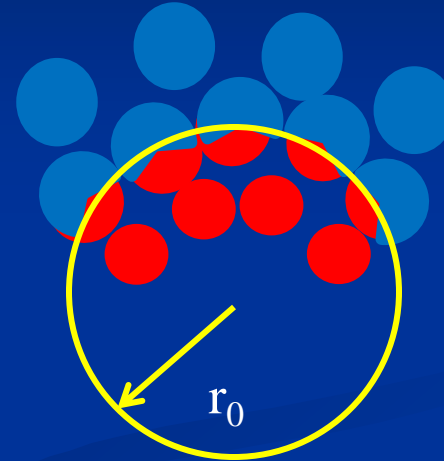
Top view

$$\kappa_0 = 0$$



$\kappa_0$  : Optimal curvature.

$$\kappa_0 = -1/r_0$$



disordered  
chain

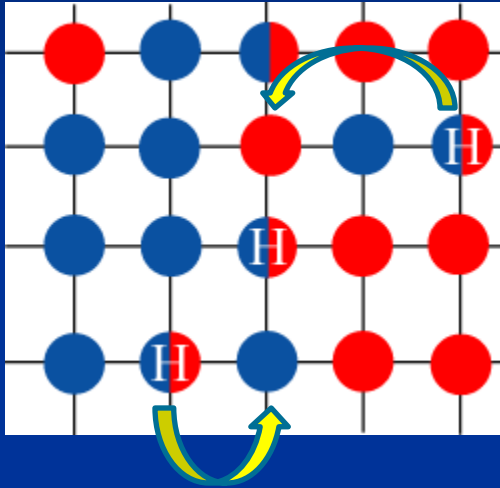
ordered  
chain

- Spontaneous curvature determines radius of domains stabilized by
- Subject to conservation constraints of S, U, and H (microemulsion)
- R. Brewster, SAS: Biophys. J. Lett., in press



# Hybrid lipid more effective in line tension reduction in S+H

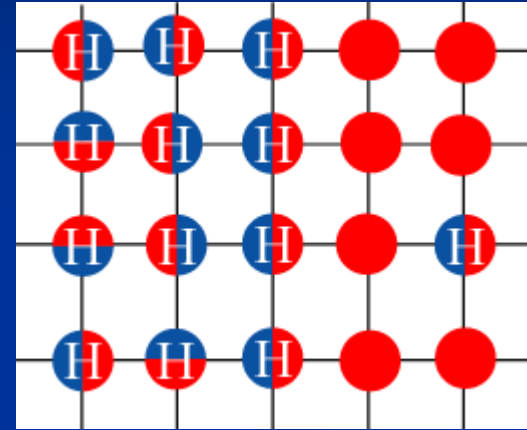
S + U membrane + H



Must bring H to interface

Cost mixing entropy:  
Only effective at low T

S + H membrane

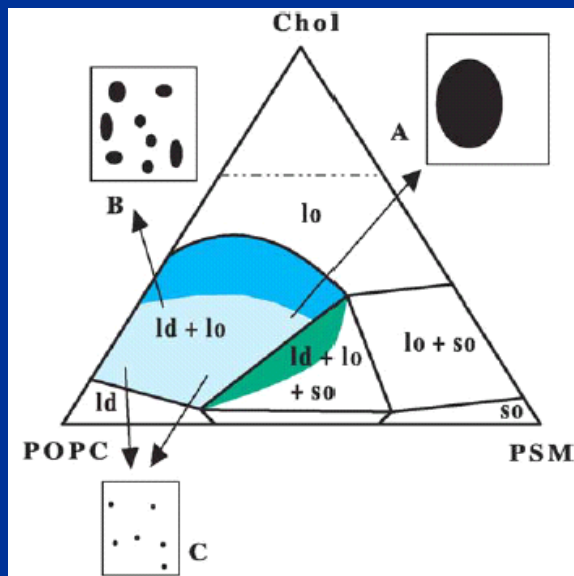


H is already there!

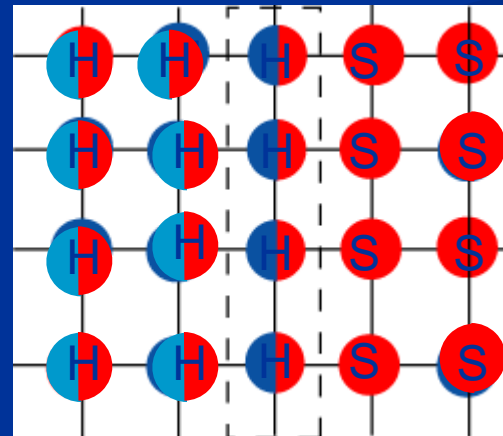
No mixing entropy cost:  
Effective even near the onset of  
the phase separation ( $T \sim T_c$ )

# Hybrid + Saturated Lipids

- Hybrid saturated chain can have different order states
- In bulk (surrounded by other H) can be disordered
- Near interface with S phase will be more ordered
- Hybrid is line active in 2 component system due to the internal degree of freedom of chain order



(Almeida et al., JMB 2005)

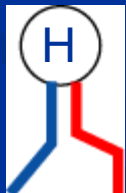


bulk: saturated chain of H disordered  
 interface: saturated chain of H ordered  
 H can be line active

Line active



Bulk



# Expts: Hybrid + Saturated

- **Macroscopic or small domains**
  - **S+U+C** clearly macroscopic
  - **S+H+C** ???
- Membranes of POPC, Palmitoyl SM, and cholesterol phase separate, in large domains  
(Veatch and Keller PRL 94, 148101 (2005))
- Type I (sat, unsat, chol) – macroscopic phase separation  
Type II (sat, hybrid, chol) – nanometric domains  
(Feigenson, Biochimia Biophys Acta, 2009)
- Ziblat et al. – POPC needed to stabilize the membrane for experiments

Almeida et al., JMB 2005  
Silva et al. – to be published

