Magnetic Dipole Interaction

Electronic Spins

$$H_{spin-spin} = \hbar \xi (3(\hat{r} \cdot \vec{\sigma})_1 (\hat{r} \cdot \vec{\sigma})_2 - \sum_{k=x,y,z} \sigma_{k,1} \sigma_{k,2})$$

$$\xi/2\pi = \frac{13}{(r/1\mu m)^3} \quad \text{mHz}$$

- Results in entanglement
- Was never directly measured: dominated by exchange interaction
- If measured with high precision: search for anomalous spin forces

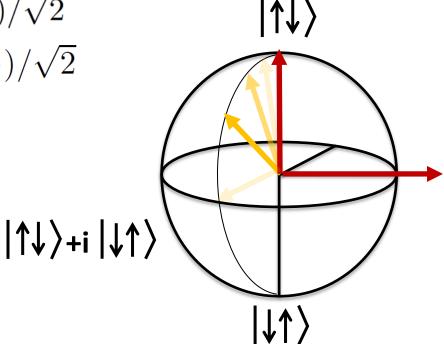


Spin-Spin eigenstates:

$$|\Psi+\rangle = (|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle)/\sqrt{2}$$

$$|\Psi-\rangle = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)/\sqrt{2}$$



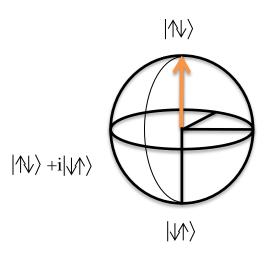


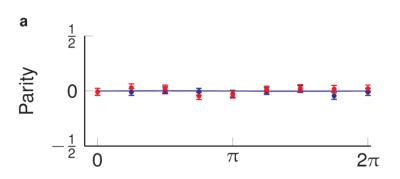
- $\Delta E = 4\xi = 3.8 \text{ mHz} \approx 200 \times 10^{-15} \text{ °K} \approx 20 \times 10^{-18} \text{ eV}$
- B-field spins apply on each other 130 fT; 10⁶ < than noise



Spontaneously entangled spins

After 0.1 seconds





After 15 seconds

