

Correlation Effects and Exotic Superconductivity in Graphene Multilayers

Erez Berg

Uri Zondiner, Asaf Rozen, Raquel Queiroz, Felix von Oppen, Yuval Oreg, Ady Stern, Shahal Ilani, Pablo Jarillo-Herrero, Mati Bocarsly, Jiewen Xiao, Sameer Grover, Aviram Uri, Keshav Pareek, Binghai Yan, Dmitry Efetov, Eli Zeldov, Johannes Hofmann, Debanjan Chowdhury, Jong-Yeon Lee, Eslam Khalaf, Ashvin Vishwanath, Ari Turner, Ohad Antebi, Gal Shavit, Tobias Holder, Areg Ghazaryan, Maksym Serbin, Andrea Young, Taige Wang, Shubhayu Chatterjee, Michael Zaletel, Eyal Cornfeld, Mark Rudner



TOPOLOGICAL QUANTUM MATTER

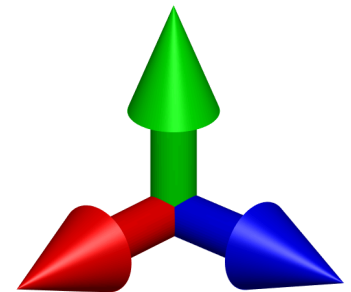
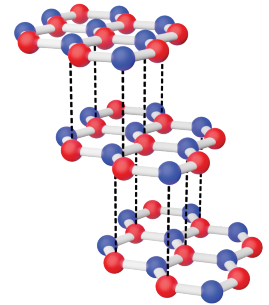
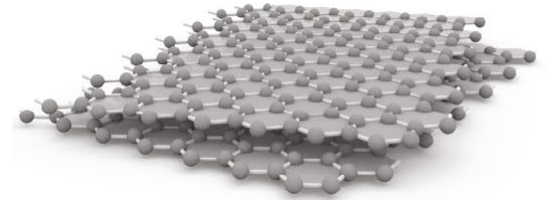


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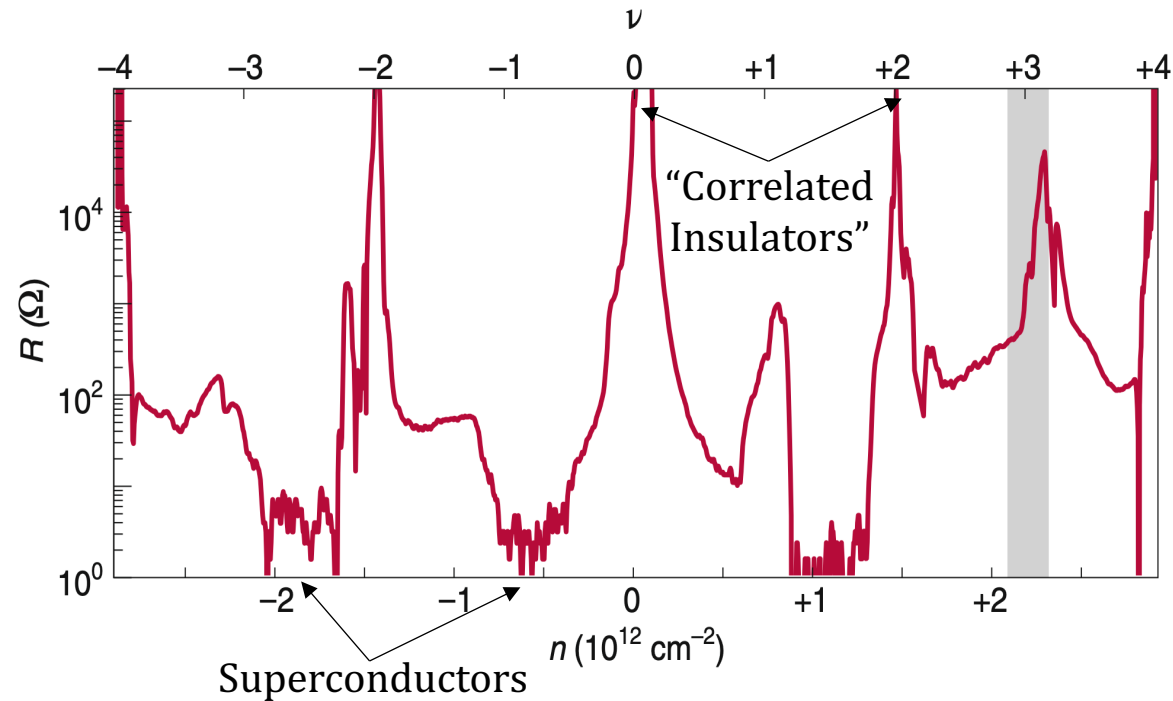
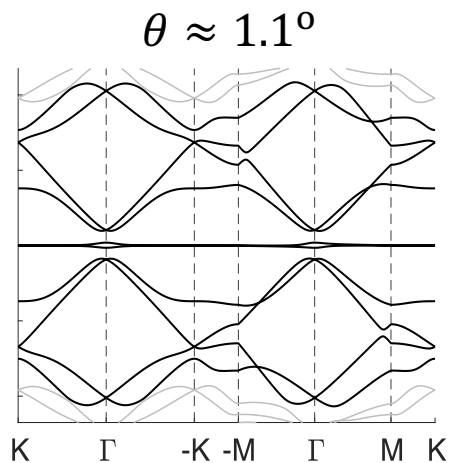
Available on: edx.org, campus.org.il
youtube.com (*coming soon!*)

Outline

- What do we know about correlation effects in magic angle twisted bilayer graphene?
- MATBG: Open Questions
- Correlations and Exotic superconductivity in Rhombohedral trilayer graphene
- Spin-polarized triplet superconductors: Order parameter topology and current dissipation



MATBG, Four years on

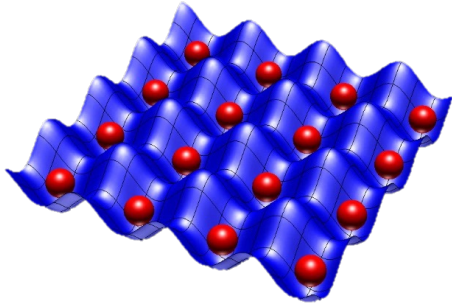


From: Balents, Dean, Efetov, Young (Nat. Phys. 2020)

What do we know for certain?

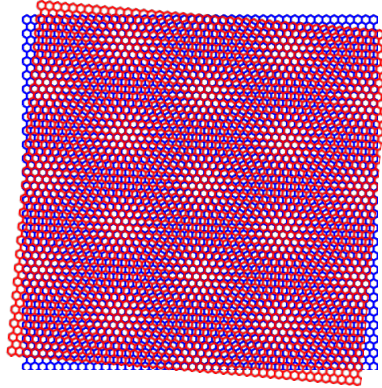
R. Bistritzer, A. MacDonald (PNAS, 2011); Y. Cao, ..., P. Jarillo-Herrero (Nature, 2019); ...

Flat Bands in MATBG

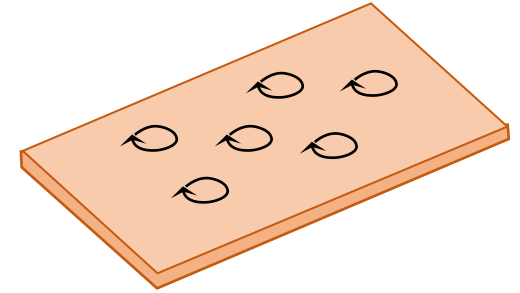


**Strong periodic
potential**

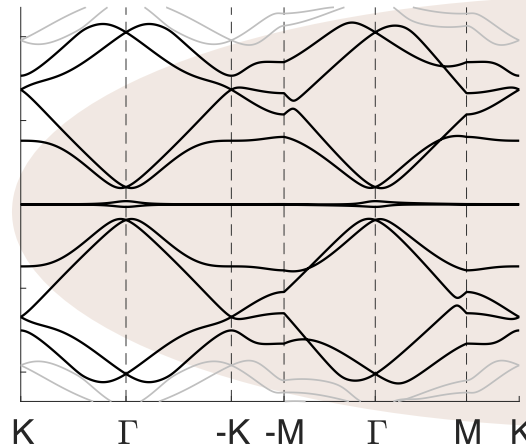
- Mott insulators
- Antiferromagnetic interactions (superexchange)
- Localized moments, unconventional superconductivity, ...



B
↑

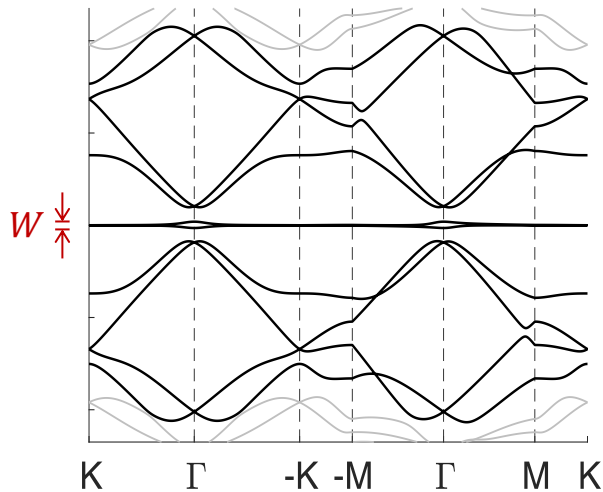


Landau levels



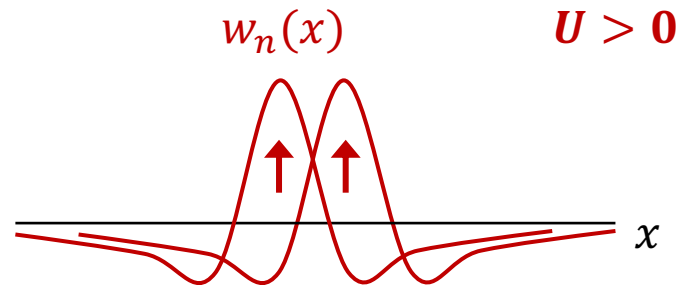
- Quantum Hall Insulators
- (Generalized) Ferromagnetism
- Skyrmions, fractional QH phases, ...

Why Generalized Ferromagnetism?



Topological bands

Wannier orbitals overlapping in space

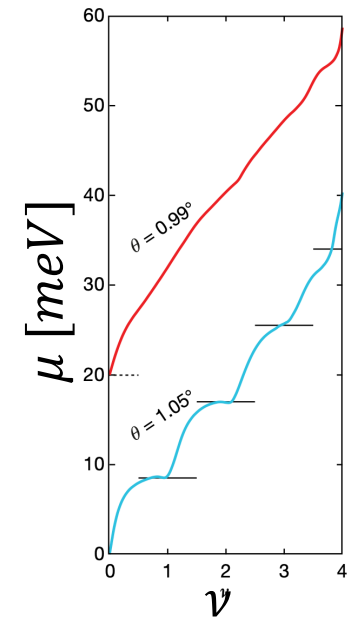
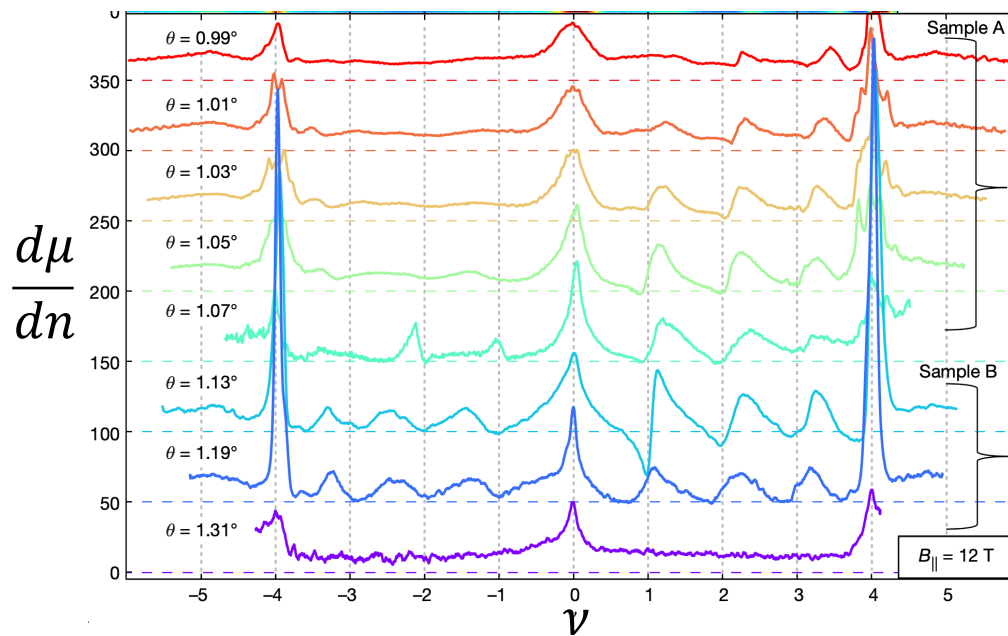
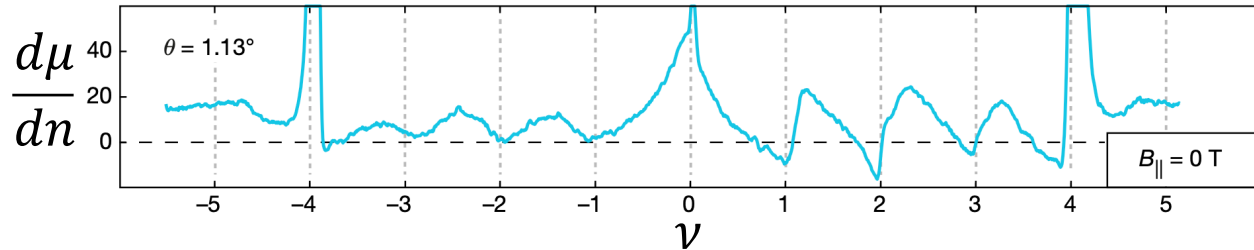


$$H = \sum_{\langle r, r' \rangle} \left(-J_F + \frac{\alpha W^2}{U} \right) \mathbf{S}_r \cdot \mathbf{S}_{r'} \quad J_F = gU, \quad g \propto \text{Wannier function overlap}$$

$$gU > \frac{\alpha W^2}{U}: \text{spin/valley ferromagnetism!}$$

Cascade of Phase Transitions

Measurements of μ and $\frac{d\mu}{dn}$ by scanning SET



"Sawtooth" features survive at least to $T \approx 50$ K!

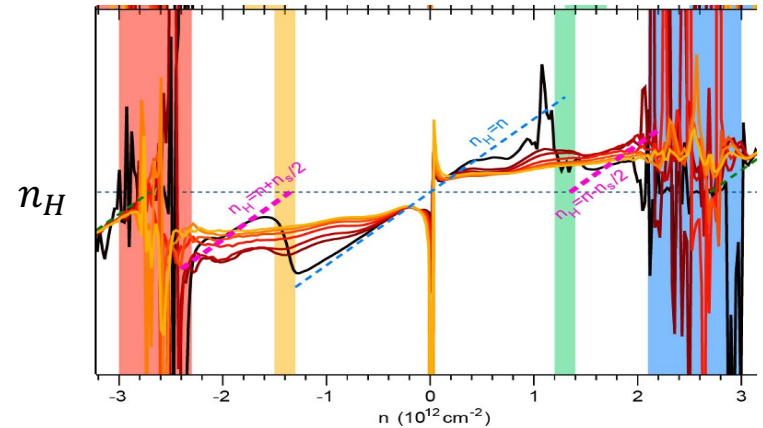
U. Zondiner, A. Rozen, D. Rodan-Legrain, Y. Cao, R. Queiroz, T. Taniguchi, K. Watanabe, Y. Oreg, F. von Oppen, A. Stern, EB, P. Jarillo-Herrero, S. Ilani (Nature, 2020)

Cascade of Phase Transitions

Fermi surface reconstruction near integer ν

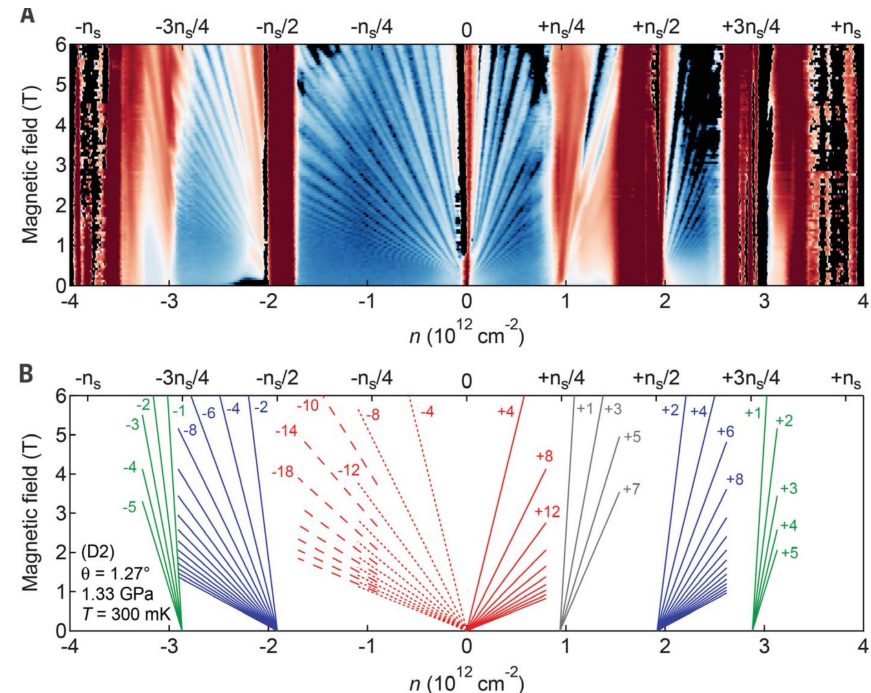
“Resets” of Hall density towards
 $n_H = 0$ at integer filling

Cao, ..., Jarillo-Herrero (Nature, 2019)



Shubnikov-de Haas oscillations:
 “Landau fans” from integer ν
 pointing away from $\nu = 0$

Yankowitz, ..., Young, Dean (Science, 2019)



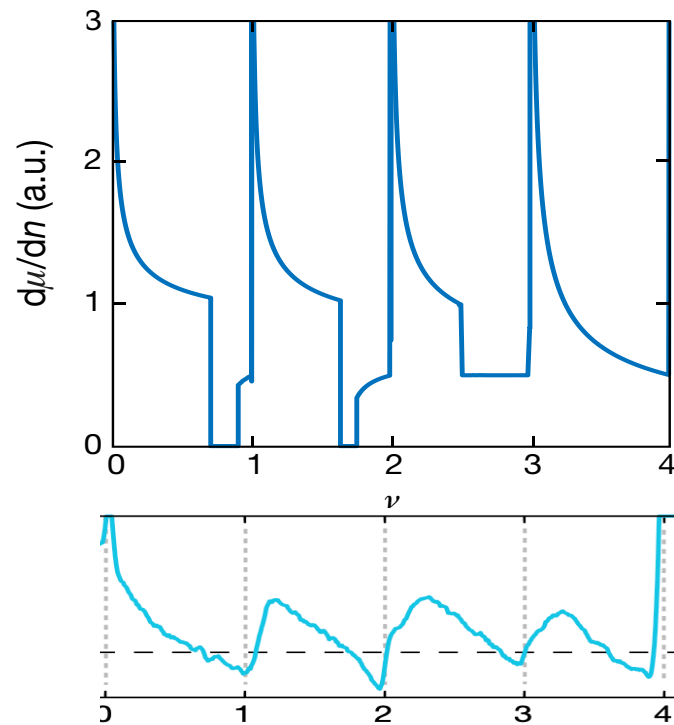
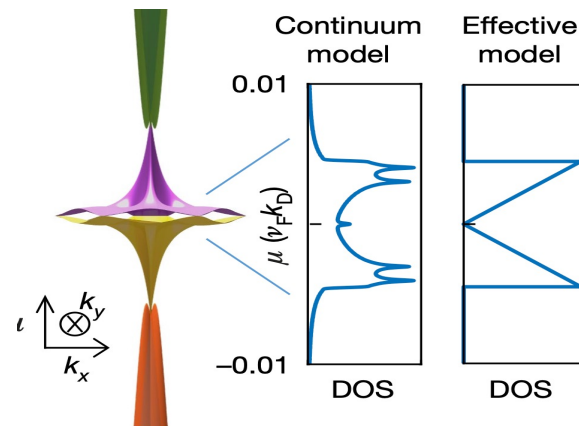
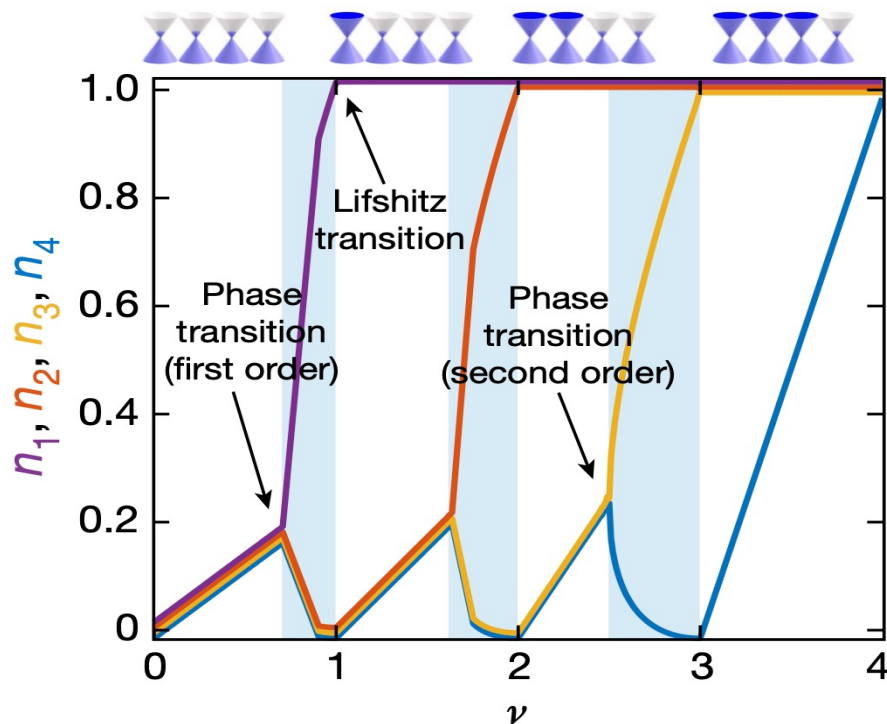
Cascade of Phase Transitions

Toy model: *U. Zondiner, ..., S. Ilani (Nature, 2020)*

$$H = \sum_{k,\alpha} \varepsilon_{\alpha k} \psi_{\alpha k}^\dagger \psi_{\alpha k} + U \int d\mathbf{r} \sum_{\alpha \neq \beta} n_{\alpha} n_{\beta}$$

$\alpha, \beta = 1, \dots, 4$ spin/valley indices

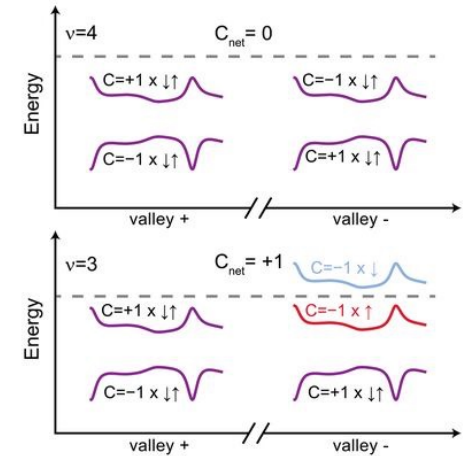
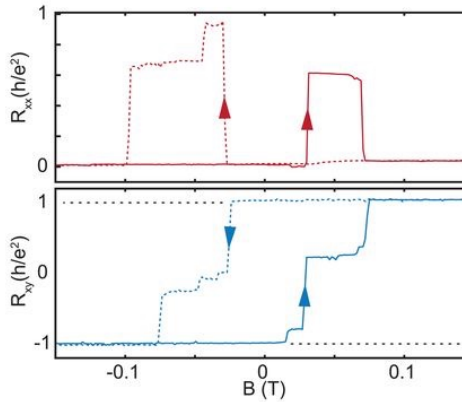
Mean-field solution:



Orbital and Spin Magnetism

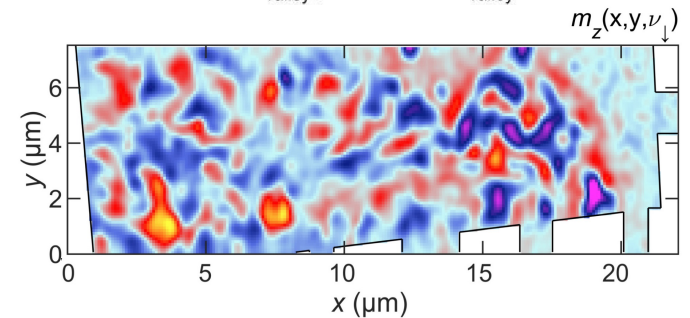
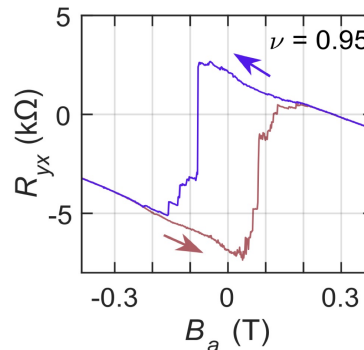
Quantized anomalous Hall
($\nu = 3$ with aligned hBN):

*Sharpe, ..., Goldhaber-Gordon
(Science, 2019);
Serlin, ..., Young (Science, 2020)*



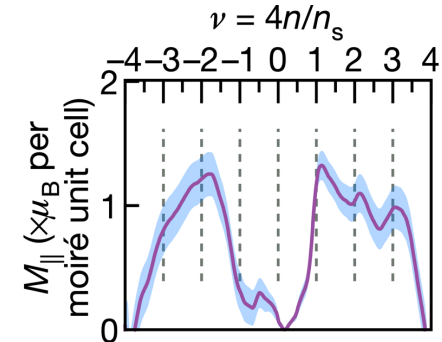
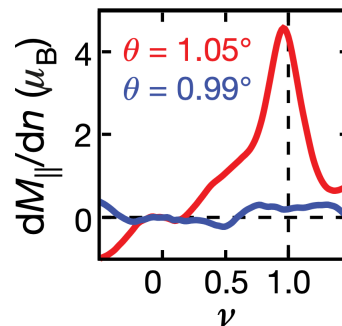
Orbital magnetism ($\nu \approx 1$):

*Grover, Bocarsly, Uri, Xiao, Yan,
..., Stern, EB, Efetov, Zeldov
(Nat. Phys., 2022)*



In-plane (spin?) magnetization: $\frac{dM_{\parallel}}{dn} = \frac{d\mu}{dB_{\parallel}}$

*Zondiner et al. (Nature, 2020);
Park et al. (Nature, 2021)*



Could have orbital component!

O. Antebi, A. Stern, EB (PRB, 2022)

Microscopic model

“Standard model” of TBLG

$$H = \hat{H}_{BM} + \hat{V}$$

$$\hat{H}_{BM} = \int d^2r c^\dagger (H_g + H_T) c \quad \hat{V} = \frac{1}{2} \sum_q V_q \delta\rho_q \delta\rho_{-q}$$

Project to narrow bands

Zero bandwidth limit ($W \rightarrow 0$)

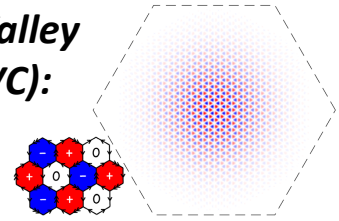
H has low-energy $U(4)$ symm.

$\nu = 0$: spin/valley polarized, KIVC state degenerate

$0 < W \ll V$

Kramers Inter-Valley Coherent (KIVC) state selected

**Kramers Inter-Valley
Coherence (KIVC):**



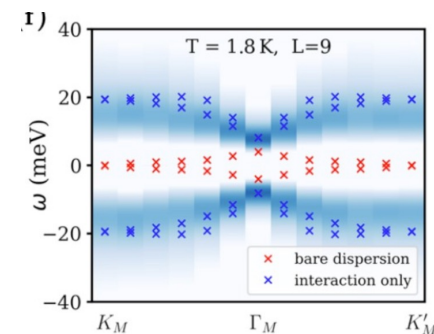
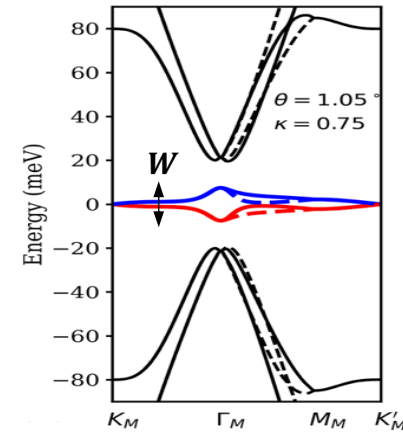
*Bultnick, Vishwanath,
Zaletel et al. (PRX, 2020)*

Quantum Monte Carlo (no sign problem @ $\nu = 0$)

Gapped KIVC state at magic angle

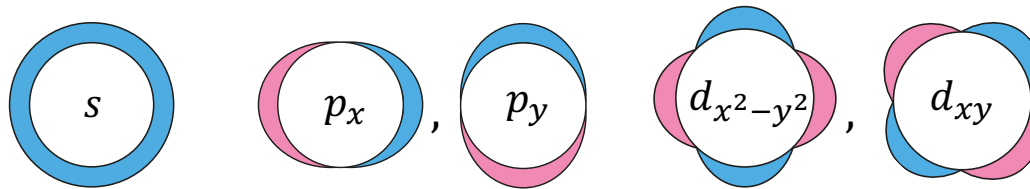
Continuous transition to semi-metal at $\theta \approx 1.25^\circ$

J. Hofmann, E. Khalaf, A. Vishwanath, EB, J. Y. Lee (PRX, 2022)

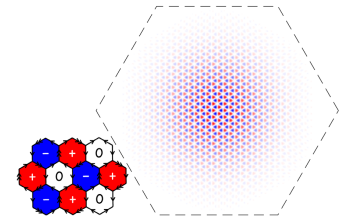


Challenges and Open Questions

- What is the nature of superconductivity?
- *Symmetry of the superconducting order parameter?*

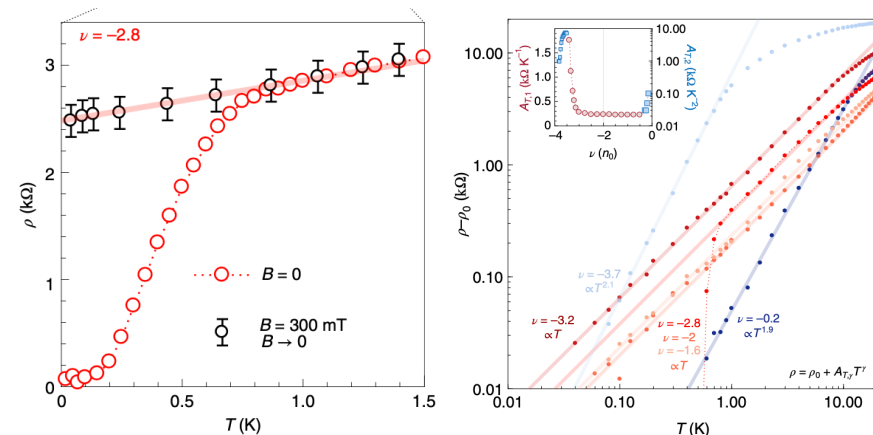


- What is the nature of the insulating states at even ν ? Broken symmetry?
- *KIVC state?*



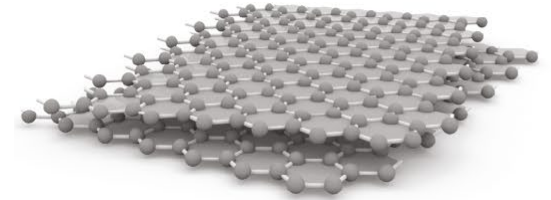
- Normal state: Fermi liquid?
“Strange metal”?
- $\rho(T) = \rho_0 + AT$ as $T \rightarrow 0$?

Cao, Chowdhury,..., Jarillo-Herrero (PRL, 2020);
Jauoi, Das,..., Efetov (Nat. Phys., 2022)



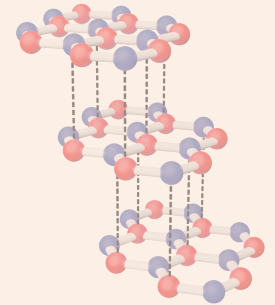
Outline

- What do we know about correlation effects in magic angle twisted graphene?

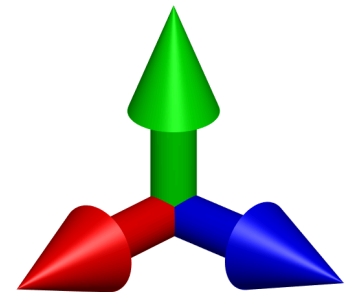


- MATBG: Open Questions

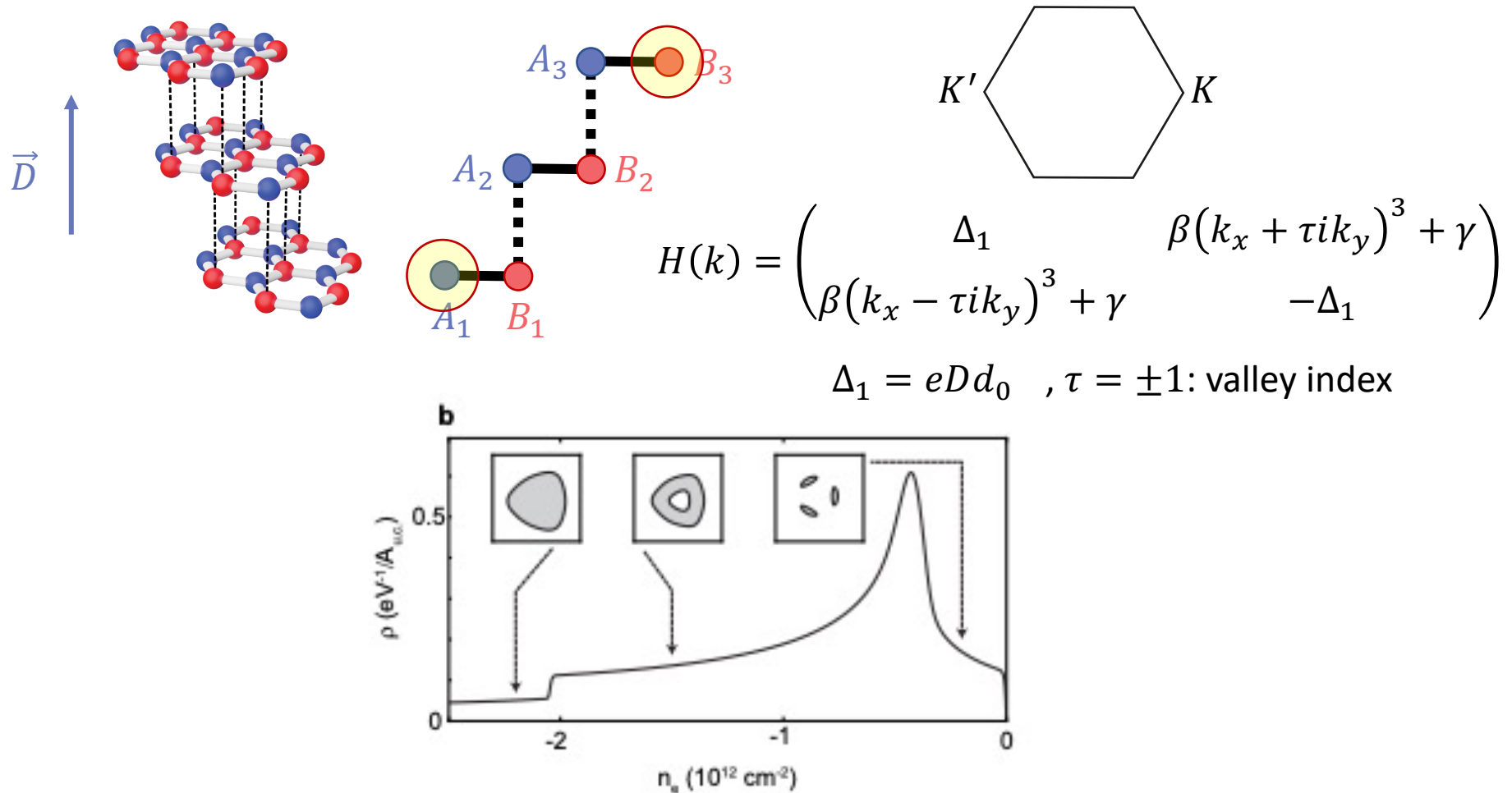
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Rhombohedral (ABC) trilayer graphene

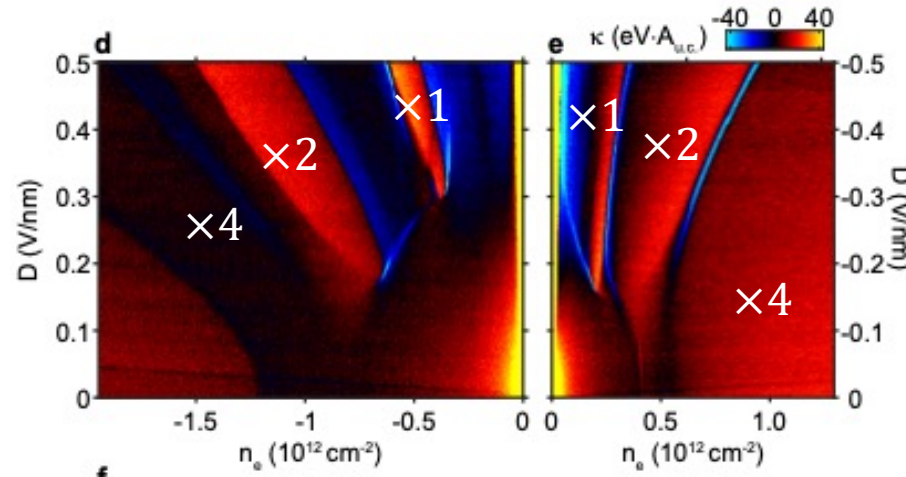


Koshino, McCann (2009); Zhang, Sahu, Min, McDonald (2010)

Phase diagram

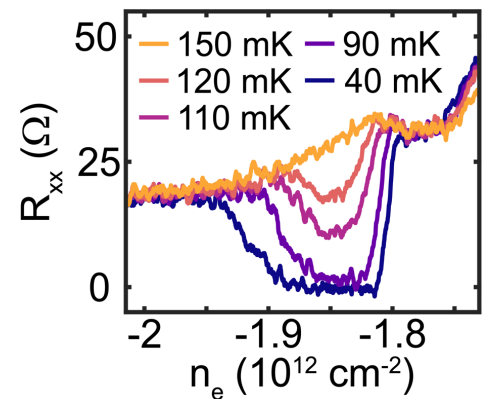
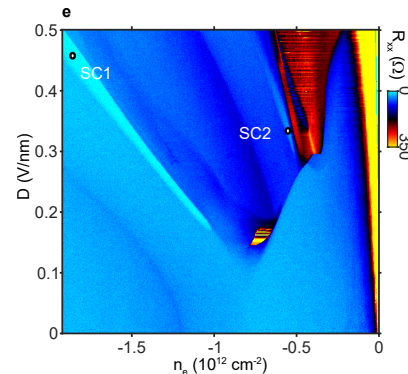
H. Zhou, ..., A. Ghazaryan T. Holder, EB, M. Serbyn, A. Young, Nature (2021)

Cascade of symm-breaking transitions (analogous to TBLG: Zondiner et al., 2020)



Superconductivity!

- Two phases SC1, SC2
 $T_{c,1} \approx 100 \text{ mK}$, $T_{c,2} \approx 50 \text{ mK}$
- SC1: (probably) spin singlet,
SC2: spin triplet!



Zhou, Xie, Taniguchi, Watanabe, Young, Nature (2021)

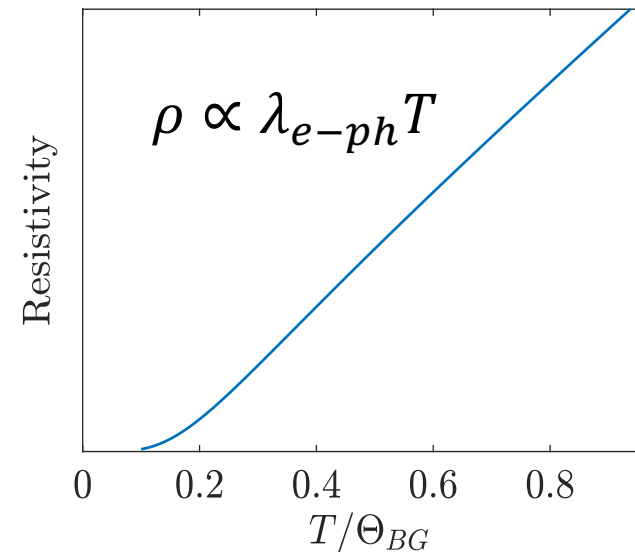
Puzzles

Conventional (acoustic phonon-mediated) s-wave?

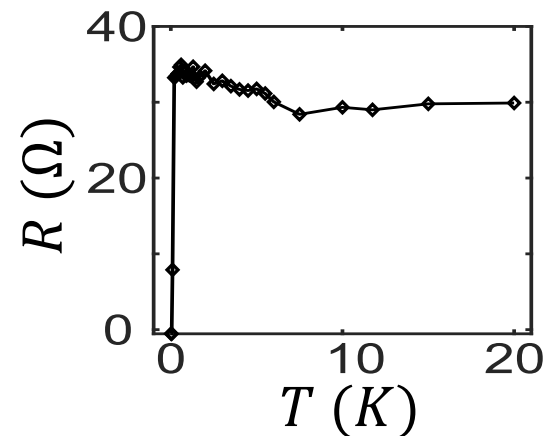
Chou, Wu, Sau, Das Sarma (2021)

$$\Theta_{BG} = 2v_s k_F \approx 40\text{K}$$

Resistivity should be
linear in T for $T \gtrsim \Theta_{BG}/4$



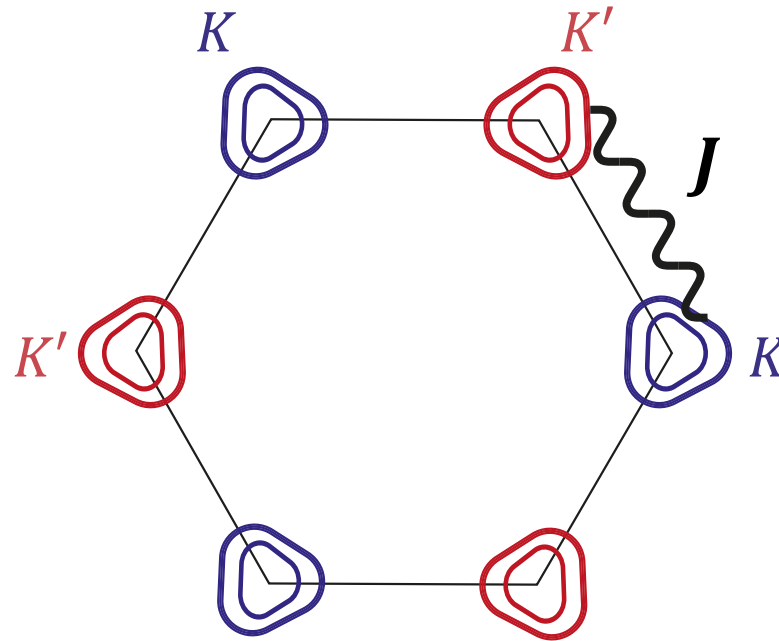
H. Zhou et al. (2021)



Puzzles (2)

Singlet or triplet?

$$H_J = -J \int d^2r \vec{S}_K \cdot \vec{S}_{K'}$$



SC2: normal state is spin-polarized $\Rightarrow J > 0$, triplet SC

SC1: normal state is spin-unpolarized \Rightarrow singlet SC??

Electronic mechanism

NEW MECHANISM FOR SUPERCONDUCTIVITY*

W. Kohn

University of California, San Diego, La Jolla, California

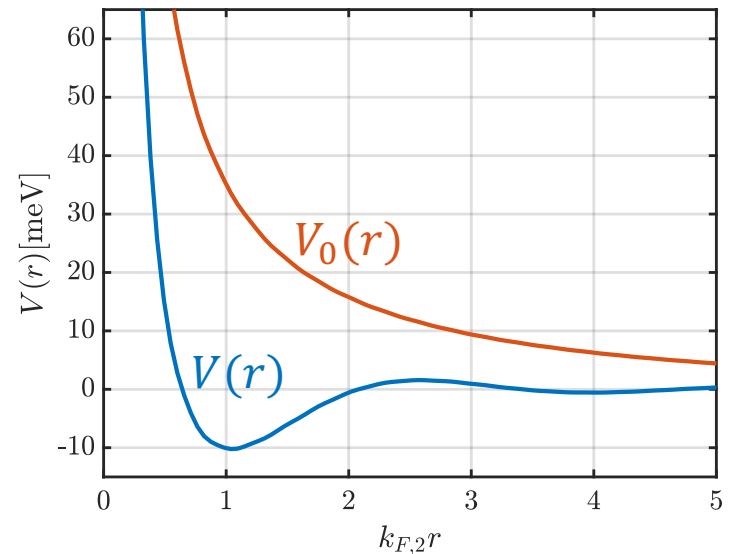
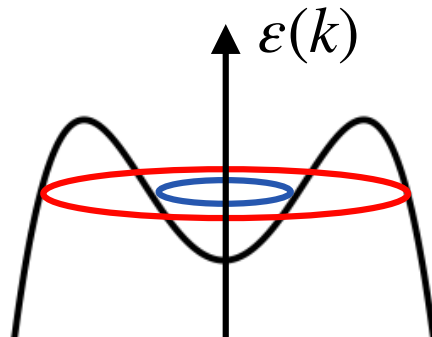
and

J. M. Luttinger (1965)

Screened Coulomb interaction (RPA):

$$V_{\mathbf{q}} = \text{wavy line} = \text{wavy line} + \text{wavy line} \begin{array}{c} \text{---} a \text{---} \\ \text{---} a \text{---} \end{array} \text{wavy line} \\ + \text{wavy line} \begin{array}{c} \text{---} a \text{---} \\ \text{---} a \text{---} \end{array} \text{wavy line} \begin{array}{c} \text{---} b \text{---} \\ \text{---} b \text{---} \end{array} \text{wavy line} \\ + \dots = \frac{V_{0,q}}{1 + N \Pi_{0,q} V_{0,q}}$$

Annular 2D
Fermi surface



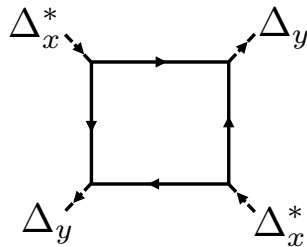
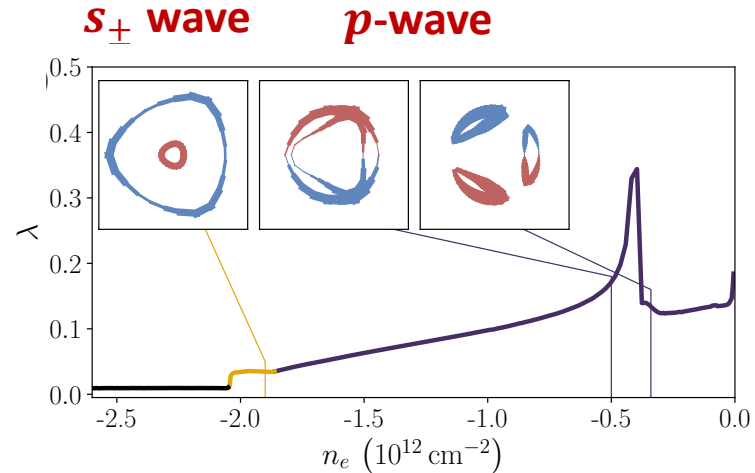
Results

Solution to the linearized BCS gap equation with V_q

$$\Gamma = \begin{array}{c} a \rightarrow \text{---} \rightarrow a \\ b \rightarrow \text{---} \rightarrow b \end{array} \text{ (shaded box)} = \begin{array}{c} a \rightarrow \text{---} \rightarrow a \\ b \rightarrow \text{---} \rightarrow b \end{array} \text{ (wavy)} + \begin{array}{c} a \rightarrow \text{---} \rightarrow a \\ b \rightarrow \text{---} \rightarrow b \end{array} \text{ (double wavy)} + \dots$$

$$T_c = W e^{-1/\lambda}$$

$$W \sim E_F$$



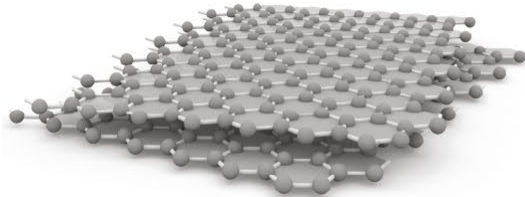
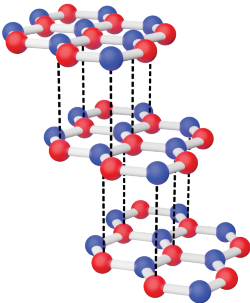
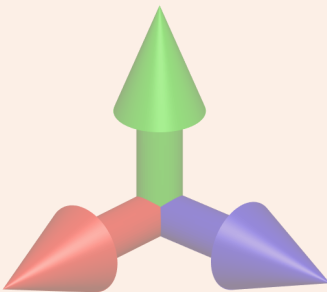
Beyond the linearized BCS equation:

Chiral $\Delta_x + i\Delta_y$

$$\text{(Diagram 1)} + e^{2\pi i/3} \text{(Diagram 2)} + e^{4\pi i/3} \text{(Diagram 3)}$$

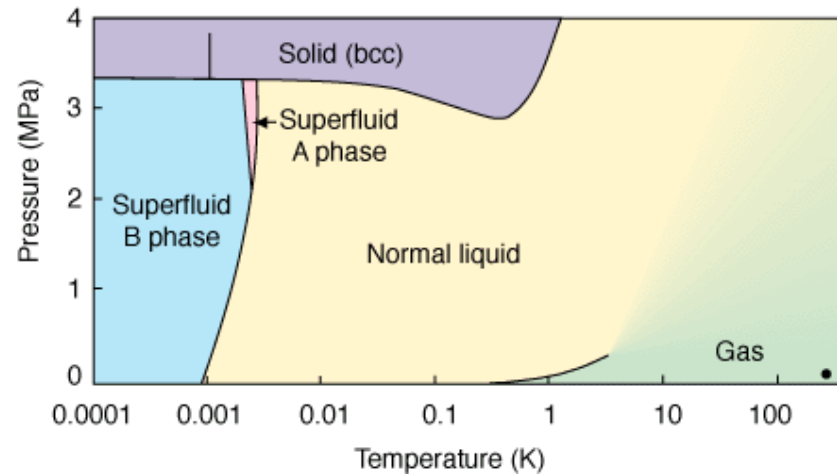
- e-e scattering conserves momentum: $\rho(T > T_c) \approx \text{const.}$
- Coulomb interactions favor spin singlet for SC1

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- 
- 
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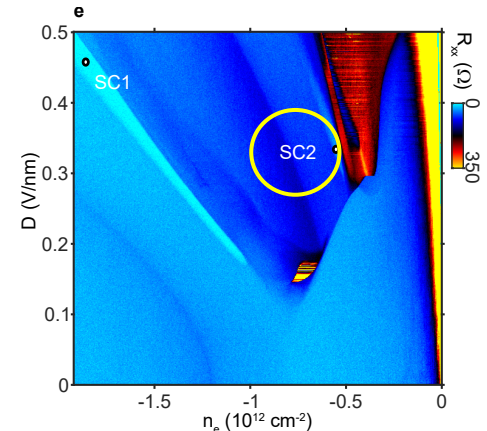
Triplet superconductivity in RTG

Solid state analogue
of superfluid ^3He ?



Triplet superconductivity:

- Strong electronic correlations ✓
- Nearby/coexisting ferromagnetism ✓
- Extremely clean ✓



Very small spin-orbit: SC and magnetism
intertwined in interesting way?

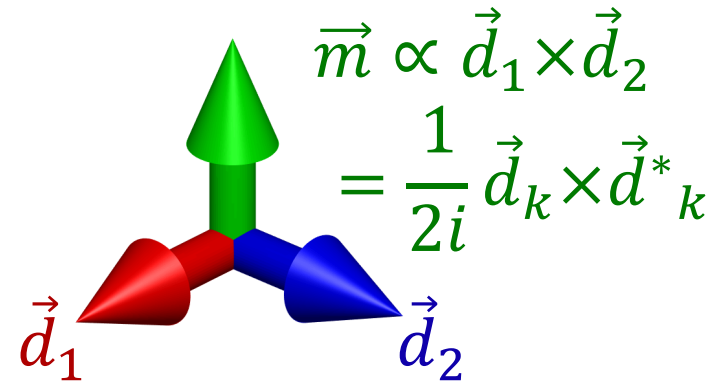
Order parameter of a spin-polarized superconductor

Order parameter of a spin-triplet SC:

$$\vec{d}_k = \langle c_k^\dagger i\sigma_2 \vec{\sigma} c_{-k}^\dagger \rangle \equiv \vec{d}_{1,k} + i\vec{d}_{2,k}$$

Fully spin polarized SC: $|\vec{d}_{1,k}| = |\vec{d}_{2,k}|$, $\vec{d}_{1,k} \perp \vec{d}_{2,k}$

Order parameter space: $SO(3)$
(Neglecting spin-orbit coupling)

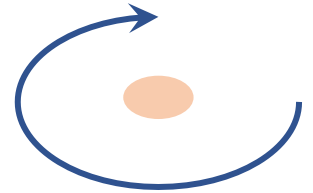


No finite T transition in $d = 2$
Mukerjee, Xu, Moore (2006)

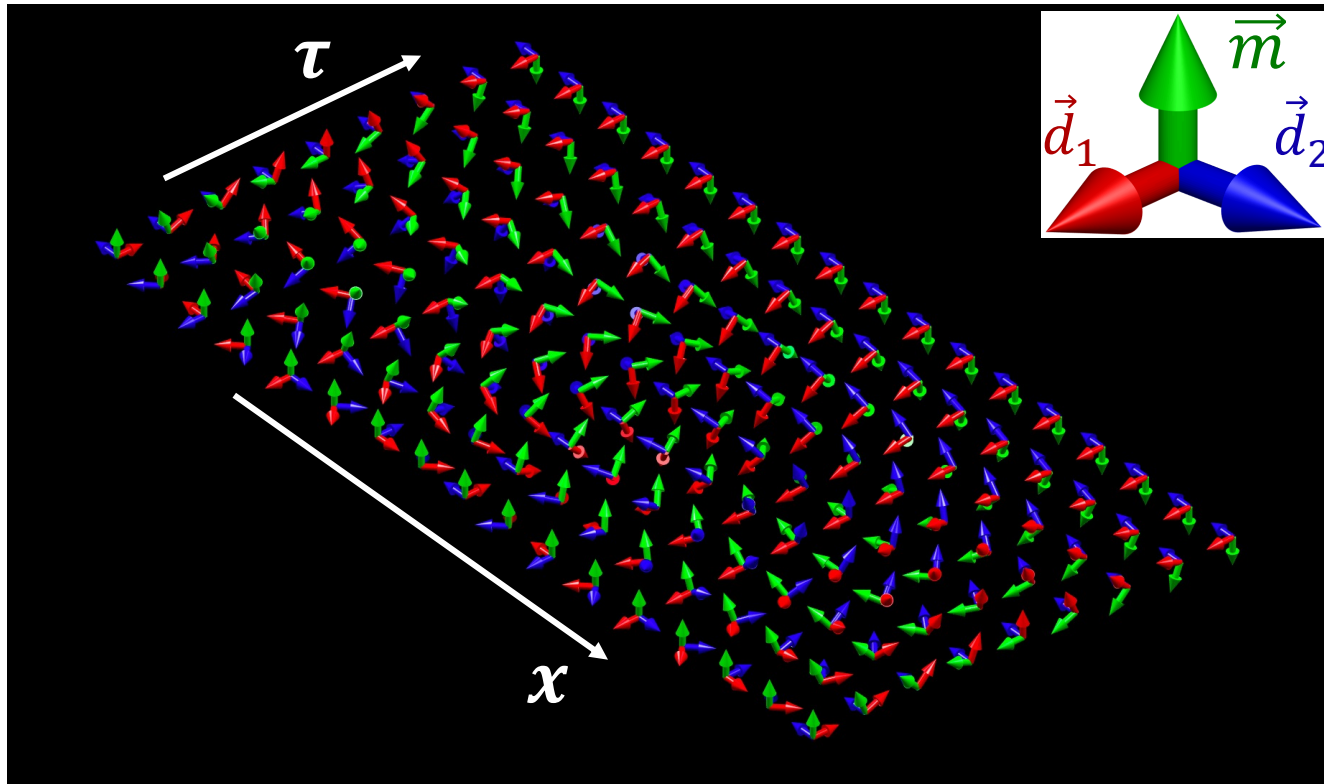
Topological defects

Polarized triplet superconductor:

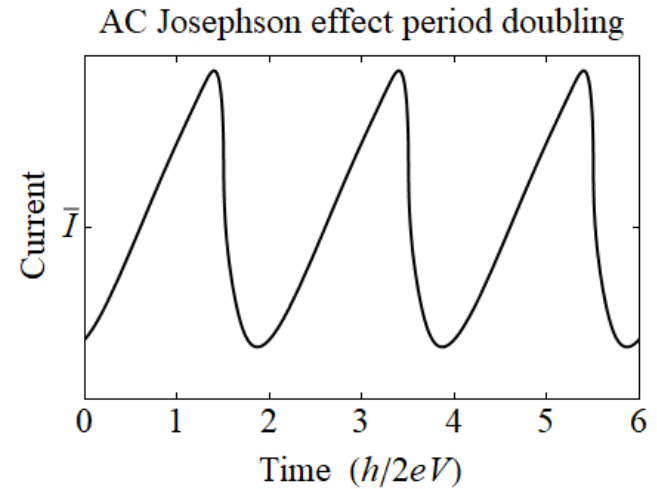
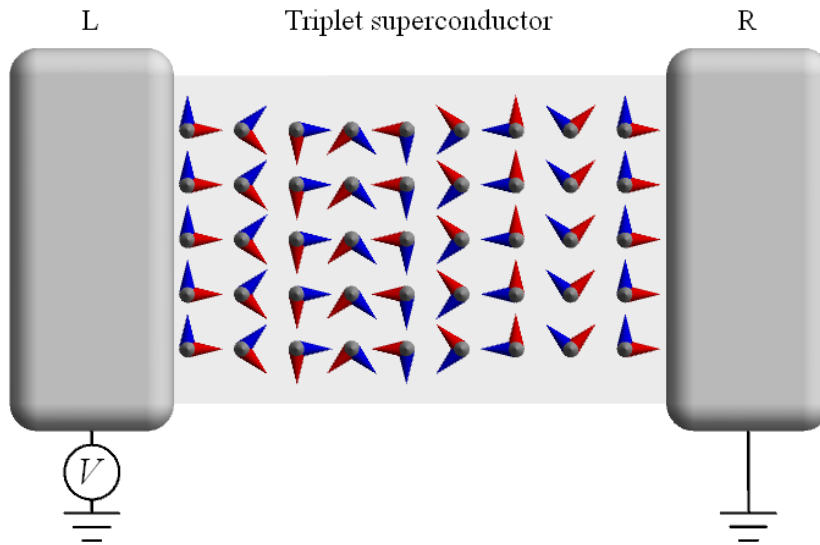
$$\pi_1(SO(3)) = Z_2 \quad (Z_2 \text{ superconducting vortex})$$



Unwinding a phase twist of 4π :



Double-period Josephson effect



Half the usual Josephson frequency: $\omega = \frac{eV}{\hbar}$

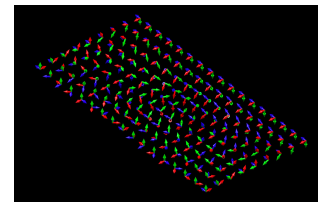
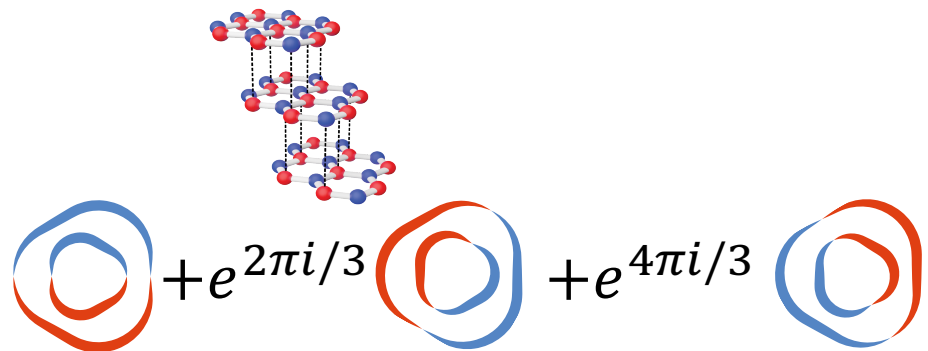
Critical current: $J_c \sim 1/\lambda \sim \sqrt{B}$

**T is low enough such that vortex-antivortex dissociation is suppressed.*

Summary

Astonishingly rich correlated electron phenomena in multilayer graphene!

- **MATBG:** Cascade of phase transitions, spin/valley ferromagnetism, Chern insulators
- **Open questions:** Symmetry of SC order parameter? Broken symmetry at even ν ? Non-Fermi liquid?
- **Unconventional SC in ABC trilayer graphene?**
Most likely state: chiral p-wave
- **Fully spin polarized SC:** fragility of supercurrent due to topology, double-period Josephson effect



Thank you!