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THE WEIZMANN INSTITUTE OF SCIENCE  
FACULTY OF MATHEMATICS AND COMPUTER SCIENCE  
Superalgebra Theory and Representations Seminar

on Wednesday, Nov 17, 2021 at 19:15

Zoom: <https://us02web.zoom.us/j/88189258443?pwd=S3JLcElXTUpadktqZ0VlWHNmVXdjQT09>

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The nilpotent cone for classical simple Lie superalgebras

Abstract:

Many aspects of the representation theory of a Lie algebra and its associated algebraic group are governed by the geometry of their nilpotent cone. In this talk, we will introduce an analogue of the nilpotent cone  $N$  for Lie superalgebras and show that for a simple classical Lie superalgebra the number of nilpotent orbits is finite. We will also show that the commuting variety  $X$  described by Duflo and Serganova, which has applications in the study of the finite dimensional representation theory of Lie superalgebras, is contained in  $N$ . Consequently, the finiteness result on  $N$  generalizes and extends the work on the commuting variety. For the general linear Lie superalgebra  $\mathfrak{gl}(m|n)$ , we will also discuss more detailed geometric results of  $N$ . In particular, we compute the dimensions of  $N$  and the centralizer of a nilpotent orbit, describe the irreducible components of  $N$ , and show that  $N$  is a complete intersection. This is joint work with Daniel Nakano from the University of Georgia.