On rings stable under derivations

Abstract:

Let z be an algebraic function of n variables and $A(z)$ the algebra generated by all variables and all partial derivatives of z (of all orders). If z is a polynomial then $A(z)$ is just a polynomial algebra, but when z is not a polynomial then it is not clear what is the structure of this algebra. I'll report on known cases and formulate a conjecture.